# A Comparison of Alternative Models for Estimating School Performance in Mathematics and Reading/Language Arts in Four State Accountability Systems: 

Oregon Results

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## Table of Contents

Background and Introduction ..... 1
General Method Description. ..... 1
Sample. ..... 1
Instruments. ..... 1
School Performance Models ..... 2
Percent proficient ..... 2
Average gain score ..... 2
Transition matrix ..... 2
Student growth percentiles ..... 3
Value-added models. ..... 3
Multilevel Linear Growth Model Initial Status, Focal Year Growth, and Average Growth (MLM0, MLM Growth Rate and MLM Average Growth Rate ..... 3
Comparison of Model Estimates ..... 4
Comparison of School Ranks Based on Model Estimates. ..... 4
Summary ..... 5
Oregon Study ..... 6
Method. ..... 6
Sample ..... 6
Instrument ..... 8
Results and Discussion. ..... 8
Section A: School Performance Estimates. ..... 8
Cohort stability. ..... 8
Comparison of models ..... 10
Relation with school composition variables. ..... 13
Relation of model estimates to SWD school composition. ..... 15
Summary of Section A. ..... 16
Section B: School Ranks Based on School Performance Estimates. ..... 16
Comparison of cohorts ..... 17
Comparison of models ..... 25
Relation with school composition variables. ..... 35
Relation of school ranks with SWD school composition. ..... 37
Summary of Section B ..... 38
Conclusion ..... 38
References ..... 40
Appendix A. Correlations among School Performance Model Estimates for Each Individual Cohort by Content Area and Grade Level Band ..... 41
Appendix B. Correlations of School Performance Model Estimates with School Composition Variables for each Individual Cohort by Content Area and Grade Level Band. ..... 46
Appendix C. Correlations of School Performance Model Estimates with School
Percentage SWD for each Individual Cohort by Content Area and Grade Level Band. ..... 50
Appendix D. Proportion of Elementary or Middle Schools within 5, 10, or 20 Ranks of Each Other for each Pair of School Performance Models in Mathematics and Reading Comprehension by Cohort.51
Appendix E. RMSD in School Ranks for Pairs of School Performance Models for each Individual Cohort by Content Area and Grade Level Band ..... 60
Appendix F. Correlations of School Ranks with School Composition Variables by Content Area and Grade Level Band for each Individual Cohort ..... 64
Appendix G. Correlations of School Ranks with School Percentage SWD for each individual Cohort by Content Area and Grade Level Band ..... 70

## List of Tables

$$
\begin{aligned}
& \text { 1. Proportion and Standard Deviation (in parentheses) of Student Subgroups for the } \\
& \text { Oregon Analytical Samples by Content Area and Grade Level Band................. } 7
\end{aligned}
$$

2. Correlations of School Performance Model Estimates Across Cohorts by Content Area and Grade Level Band. ..... 9
3. Average Correlations across Content Area and Grade Level Band and Overall Mean and Standard Deviation (SD) Across the Three Cohort Comparisons. ..... 10
4. Correlations of School Performance Estimates across Models by Content Area and Grade Level Band. ..... 11
5. Correlations of School Performance Model Estimates between Mathematics and Reading Comprehension by Grade Level Band in each Cohort and Averaged over Cohorts. ..... 13
6. Correlations of Model Estimates with School Composition Variables by Content Area and Grade Level Band. ..... 14
7. Average School Performance Model Estimates as a Function of the Percentage of SWD in the School by Content and Grade Level Band. ..... 15
8. Spearman's Correlations of Model School Ranks for Each Pair of Cohorts by Content Area and Grade Level Band. ..... 17
9. Spearman's Correlations of Model School Ranks Averaged Across Content Area and Grade Level Band and Overall Mean and Standard Deviation (SD) Across the Three Cohort Comparisons ..... 18
10. Proportion of Elementa
ry or Middle Schools Within 5, 10, or 20 Ranks of Each Other for Each School Performance Model for Each Pair of Cohorts in Mathematics and Reading ..... 19 Comprehension.11. RMSD in School Ranks for Each Student Cohort for Each School PerformanceModel by Content Area and Grade Level Band.24
11. Proportion of Elementary or Middle Schools Within 5, 10, or 20 Ranks of Each Other for Each Pair of School Performance Models in Mathematics and Reading Comprehension Averaged Over Cohorts. ..... 26
12. Average Across Cohorts of RMSD in School Ranks Between School Performance Models by Content Area and Grade Level Band. ..... 32
13. Spearman's Correlations of School Performance Model Estimates Across Mathematics and Reading Comprehension by Cohort. ..... 33
14. Proportion of Elementary or Middle Schools Within 5, 10, or 20 Ranks of Each Other in Mathematics versus Reading Comprehension for Each School Performance Model Averaged Over Cohorts. ..... 34
15. RMSD in School Ranks for Mathematics and Reading Comprehension by Cohort and Grade Level Band and Overall Means and Standard Deviations (SD) ..... 35
16. Spearman's Correlations of School Ranks With School Composition Variables by Content and Grade Level Band. ..... 36
17. Average School Rank as a Function of the Percentage of SWD in the School by Model, Content Area, and Grade Level Band ..... 37

## A Comparison of Alternative Models for Estimating School Performance in Mathematics and Reading/Language Arts in Four State Accountability Systems: Oregon Results

## Background and Introduction

This technical report is one of a series of four technical reports that describe the results of a study comparing eight alternative models for estimating school academic achievement using data from the Arizona, North Carolina, Oregon, and Pennsylvania accountability systems. Our purpose was not to evaluate or examine the accountability systems in use by these states, but to evaluate a broader range of models commonly used for estimating school performance that are applied in many states and frequently reported in the school effectiveness research literature. This introduction briefly describes the study background and details the methods and procedures we used to estimate the eight school performance models and compare model results in all four states. The individual state technical reports including details on each state's accountability data, assessment instruments, and results are provided at: http://www.ncaase.com/publications/techreports.

Despite the central importance of analytic models used in evaluating teacher and school effects in modern accountability systems, there are relatively few studies of the reliability and validity of these high-stakes systems (see, for example, Goldschmidt, Choi, \& Beaudoin, 2012). The results reported here examine eight models using operational state accountability data in mathematics and reading/language arts from the four participating states. We addressed four questions surrounding the use of analytic models for the evaluation of school performance:

1. Are estimates of school performance stable across successive cohorts of students?
2. How well do estimates of school performance correlate among models?
3. How do estimates of school performance correlate with variables describing the student composition of the school?
4. Do estimates of school performance vary from one model to another based on the school composition of students with disabilities (SWD)?

## General Method Description

## Sample

The sample from each state is described in each individual state technical report. In three of the four states, the sample consisted of all students who took the state's mathematics or reading/language arts general assessment in any one school year from 2007-08 through 2011-12, and whose records in each year were included in the state's calculation of Adequate Yearly Progress (AYP). Samples were separated into two grade level bands: a longitudinal elementary school sample (Grades 3 through 5) and a longitudinal middle school sample (Grades 6 through 8), each consisting of three cohorts (a) 2007/08 through 2009/2010; (b) 2008/09 through 2010/11; and (c) 2009/10 through 2011/12 (see research design schematic below). In Arizona, only one elementary and middle school cohort was used (2006/07 through 2008/09) due to changes in the Arizona testing program that occurred in 2010.

## Instruments

The outcome measures for all analyses were the standardized mathematics and reading/language arts tests used for accountability in each state. In three of the states, the instruments used vertically linked developmental scales created using item response theory (IRT) methods. In Pennsylvania, the test was not vertically linked over grades preventing the estimation of some of the school performance models described in the next section. More detail about the Oregon test is contained in a later section of this report.

Research design indicating academic years and longitudinal cohorts studied:

| Grade | Academic Year |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2007/08 | 2008/09 | 2009/10 | 2010/11 | 2011/12 |
| 3 |  |  |  |  |  |
| 4 |  |  |  |  |  |
| 5 |  |  |  |  |  |
| 6 |  |  |  |  |  |
| 7 |  |  |  |  |  |
| 8 |  |  |  |  |  |

Note. E denotes an elementary school cohort, M denotes a middle school cohort. Only one elementary and one middle school cohort were available in the Arizona data.

## School Performance Models

For all models, we estimated school performance in the last focal year (Grade 5 or 8 ) of the two grade level bands, as well as using prior years of achievement data as dictated by the particular model. We applied eight alternative analytic models of school performance to the mathematics and reading/language arts achievement data in elementary and middle school for each state. The eight school performance models were: Percent Proficient (PP), gain score (Gain), transition matrix (TM), student growth percentile (SGP), value-added model (VAM), and three Multilevel Linear Model (MLM) estimates: focal year intercept or status (MLM0), focal year growth rate (Grate), and average MLM growth rate across the three years (AvGrate).

Percent Proficient (PP). PP was the NCLB required metric used by the state that calculated the percentage of students in each school that met or exceeded state benchmarks for proficiency in either mathematics or reading/language arts in each grade.

Average Gain Score. Gain scores were calculated as the prior academic year (Grade 4 or Grade 7) scale score in mathematics or reading/language arts subtracted from the focal year scale score (Grade 5 or Grade 8):

$$
\begin{equation*}
\text { Gain }_{i}=\Delta_{i}=Y_{i t}-Y_{i(t-1)} \tag{1}
\end{equation*}
$$

where $\mathrm{Y}_{\text {it }}$ was the assessment outcome for student $i$ at time $t$. Student gain scores were averaged for each school (labeled "Gain" below).

Transition Matrix (TM). School performance estimates were computed from a table of the state's proficiency categories in the prior year crossed with the proficiency categories in the focal year (Grade 5 or Grade 8) which, in the case of five proficiency categories, created a transition matrix table of 25 cells. The percentage of students occurring in each of the cells was
entered and then a weighting scheme was applied to each cell and the products were summed to create a TM school performance index. The weighting scheme awarded one of three scores: (a) -1 was recorded if the student moved down one or more categories from the previous year, (b) 0 was recorded if the student stayed in the same category, and (c) +1 was recorded if the student moved up one or more categories from the previous year (see Tindal, Nese, \& Stevens, 2017). The weighted values were averaged across all cells to create an overall school TM index.

Student Growth Percentiles (SGP). Student growth percentiles were computed at the student level using the approach described by Betebenner (2009). A student's SGP was calculated by taking the current year test score and regressing it on the two prior years of test scores. Betebenner's (2009) approach uses ordinal methods (quantile regression) as well as Bspline, cubic polynomial smoothing of the resulting normative distribution of conditional regression estimates. The analysis results in a relative rank for each student in a conditional distribution of those who had similar scores in previous years. We used the R package $S G P$ (Betebenner, \& Iwaarden, 2011) to compute student estimates based on the regression of the two prior years of test scores on the current year's test score and then we aggregated student SGP for each school to create a median SGP as each school's SGP performance estimate.

Value-added Models (VAM). This mixed effects approach examined performance gains over years and included indicators for student membership in a particular school. This model is known generally as the "layered model" because layers of equations are added with each year of schooling (Ballou, Sanders, and Wright, 2004). For example, the model for our case with students with three years of data would be specified as follows:

$$
\begin{align*}
& Y_{0 i j}=b_{0}+u_{0}+e_{0}  \tag{2a}\\
& Y_{1 i j}=b_{1}+u_{0}+u_{1}+e_{1}  \tag{2b}\\
& Y_{2 i j}=b_{2}+u_{0}+u_{1}+u_{2}+e_{2} \tag{2c}
\end{align*}
$$

where $Y_{t i j}$ represents an assessment for student $i$ at time $t$ (grade) attending school $j$. The fixed mean for all students in the combination of grades and schools was $\mu_{t i j}$, while $e_{i j}$ was the random deviation for student $n$ from the mean, $\mu_{t i j}$. The layered model we used was limited to a maximum of three years and was applied separately to mathematics and reading/language arts.

## Multilevel Linear Growth Model Initial Status, Focal Year Growth, and Average

 Growth (MLM0, MLM Growth Rate and MLM Average Growth Rate). We modeled student growth over the three elementary or three middle school grades with multilevel longitudinal analyses (Raudenbush \& Bryk, 2002) using HLM 7.1 (Raudenbush, Bryk, Cheong, Congdon, \& du Toit, 2011) and full maximum likelihood estimation. The conditional models included a level-1 model that specified student mathematics or reading/language arts scores predicted by a quadratic function of time of measurement, a level-2 model composed of the prediction of level1 model parameters as a function of student mean values, and a level- 3 model composed of the prediction of level-2 parameters as a function of school mean parameter values. Time was centered on the focal year (Grade 5 or 8) for computation of MLM0 and MLM growth rate but was centered on the middle year (Grade 4 or 7) for computation of MLM average growth rate. We used a quadratic model based on previous findings (Bloom, Hill, Black, \& Lipsey, 2008) as well as inspection of the data and statistical testing of alternative growth functions. Because only three time points were present, the model intercept and linear slope were randomparameters but the variance of the quadratic parameter was fixed (note the omission of a residual term in equation 4 c below) to obtain a model solution. We used two different centering definitions to take into account the curvilinear nature of growth. Although centering in the last, focal year is most consistent with the definition of other models we examined, it likely underestimates the amount of growth that occurs over the three year period because of deceleration. We therefore also centered on the middle grade in the three year span to produce an average growth rate over the three years. The resulting MLM model equations were:

Level 1 (Time):

$$
\begin{equation*}
\left(Y_{t i j}\right)=\pi_{0 i j}+\pi_{1 \mathrm{ij}}\left(\operatorname{time}_{t i j}\right)+\pi_{2 i j}\left(\text { time squared }_{t i j}\right)+e_{t i j} \tag{3}
\end{equation*}
$$

Level 2 (Students):

$$
\begin{align*}
& \pi_{0 i j}=\beta_{00 j}+r_{0 i j}  \tag{4a}\\
& \pi_{l i j}=\beta_{10 j}+r_{l i j}  \tag{4b}\\
& \pi_{2 i j}=\beta_{20 j} \tag{4c}
\end{align*}
$$

Level 3 (Schools):

$$
\begin{align*}
& \beta_{00 j}=\gamma_{000}+u_{00 j}  \tag{5a}\\
& \beta_{10 j}=\gamma_{100}+u_{10 j}  \tag{5b}\\
& \beta_{20 j}=\gamma_{200}+u_{20 j} \tag{5c}
\end{align*}
$$

where $Y_{t i j}$ was the mathematics or reading/language arts scale score for student $i$ at time $t$ in school $j$, $\pi_{0 i j}$ was the initial status or intercept for student i at time 0 in school $j, \pi_{1 i j}$ was the linear rate of change, $\pi_{2 i j}$ was the quadratic curvature representing the acceleration or deceleration in each student's growth trajectory and $e_{t i j}$ was the residual for each student. At level-2, the level-1 parameters were modeled using mean parameter values across students ( $\beta_{k 0 j}$ ) and at level-3, the level-2 parameters were modeled using mean parameter values across schools $\left(\gamma_{k 0} 0_{j}\right)$.

## Comparison of Model Estimates

We used several comparison criteria to evaluate the comparability and stability of school estimates across school performance models and across cohorts. In each state technical report we describe the results of our evaluation of school performance estimates. We examined: (a) correlations of model estimates for each school across the three cohorts, (b) correlations among school estimates from one model to another, (c) correlations among the school estimates and school composition variables (e.g., percent economically disadvantaged students in the school, percent minority students in the school), and (d) correlations of each model with the percentage of students with disabilities in the school.

## Comparison of School Ranks Based on Model Estimates

Many states and districts create school ranks based on their accountability system results. To compare the alternative school performance models using this metric, we created school percentile ranks (from 1 to 99 , with 99 being the highest performance) based on each of the eight school performance model estimates described above. In one of the only studies evaluating school performance models, Goldschmidt, Choi, and Beaudoin (2012) compared models using quintiles. They examined the percentage of times schools remained in the same quintile band based on one school performance model versus another. Similarly, Castellano and Ho (2013) compared SGP and conditional regression models by examining the percentage of times schools
remained within 1,5 or 10 percentile ranks for each model. To maintain some comparability with each of these studies, we used three levels of similarity in school ranks, computing the percentage of schools within 5,10 , or 20 ranks of each other. We also computed the Spearman's correlation of school ranks from one cohort to another or from one school performance model to another. As a final comparison metric, we computed the root mean squared difference (RMSD) between school ranks based on each pair of cohorts or each pair of school performance models (see Castellano \& Ho, 2013):

$$
\begin{equation*}
R M S D_{c, c}=\sqrt{\frac{\sum_{j=1}^{j}\left(\text { Rank }_{j c}-R a n k_{j c}\right)^{2}}{n}} \tag{6}
\end{equation*}
$$

In equation 6, for a particular school performance model, the RMSD computes the difference ( $R_{a n k}{ }_{i t}$ ) between each school's rank in one cohort ( $j t$ ) versus the school's rank in a second cohort ( $j u$ ), squaring the difference, summing across all schools, dividing by the number of schools, $n$, and taking the square root of the result.

$$
\begin{equation*}
R M S D_{m n}=\sqrt{\frac{\sum\left(\text { Rank }_{j m}-\text { Rank }_{j n}\right)^{2}}{n}} \tag{7}
\end{equation*}
$$

Similarly, in equation 7, the school ranks arising from alternative school performance models are compared in which $\operatorname{Rank}_{j m}$ and $\operatorname{Rank}_{j n}$ represent the rank of school $j$ using school performance model $m$ compared to that school's rank using school performance model $n$. As in equation 6, differences in ranks are then summed, squared, divided by the number of schools and taken to the $1 / 2$ power. The RMSD was a measure of similarity in school performance models where a lower value indicates a pair of models that rank schools most similarly.

## Summary

We evaluated eight models for estimating school academic performance in mathematics and reading/language arts using operational state accountability data. In NC, OR, and PA, we examined stability in model estimates across three successive student cohorts in mathematics and reading/language arts in both elementary and middle school grades. In all four states, we also compared the estimates of school performance from one model to another to determine whether the models provided similar or different depictions of school performance, although several models could not be estimated in Pennsylvania because their state test did not use a vertically linked score scale. We then compared the degree to which model estimates correlated with variables that described the student composition of the school, a likely indication of construct irrelevant variance-ideally estimates of school performance should not be related to the student composition of the school. Last, we evaluated the school performance models in terms of the way they ranked schools, the stability of school ranks across cohorts, and the degree of agreement in school rankings from one school performance model to another. Detailed results of these analyses and comparisons follow for the state of Oregon.

## Oregon Study <br> Method

## Sample

The initial Oregon sample consisted of all students that took the Oregon Assessment of Knowledge and Skills (OAKS) mathematics ( $N=483,502$ ) or reading/language arts ( $N=$ 474,080) general assessment in any one school year from 2007-08 through 2011-12, and whose records in each year were included in the state calculation of Adequate Yearly Progress (AYP). Students who did not follow the typical grade level sequence due to grade retention, acceleration, or dubious progressions were excluded from the sample; this included the transition from 2006/07 to 2007/08, so that no students present in 2007/08 had been retained or accelerated from the previous year.

The initial sample was separated into an elementary school sample (Grades 3 through 5) and a middle school sample (Grades 6 through 8 ), each consisting of three successive cohorts of students enrolled in school years: (a) 2007/08 through 2009/2010; (b) 2008/09 through 2010/11; and (c) 2009/10 through 2011/12. The initial elementary school sample for the mathematics test was 137,744 students. The initial middle school sample for the mathematics test was 136,535 students. The initial elementary school sample for the reading/language arts test was 137,535 students. The initial middle school sample for the reading/language arts test was 137,343 students. To create an analytic sample that was appropriate for our research questions, we only included students with valid test scores in all three years, schools that served all three grades (Grades 3 through 5 or 6 through 8 ) for a cohort, and schools with $N \geq 10$ students in each of the three cohorts in the final reference year of the three-year grade level band (i.e., Grade 5 for elementary grades 3 to 5 and Grade 8 for middle grades 6 to 8 ). Students and schools that did not meet these criteria were excluded from analyses. As is the case in most operational and research applications of these models, we made no attempt to account for student mobility in years prior to the focal year or to make any attributions of "school effects" based on how many years the student had been in the focal year school. Our concern in creating the analytic sample was to maximize the interpretation of comparisons of the models rather than to ensure complete representativeness of the samples. These inclusion rules were applied to ensure that there were no differences in the analytic samples for different school models so that comparisons of school models were a function only of differences in the models and not the composition of the sample analyzed. The final elementary school analytic sample for the mathematics test was 90,679 students ( $65.8 \%$ of the initial sample). The final middle school analytic sample for the mathematics test was 75,318 students ( $55.2 \%$ ). The final elementary school analytic sample for the reading/language arts test was 89,627 students ( $65.2 \%$ ). The final middle school analytic sample for the reading/language arts test was 75,193 students ( $54.7 \%$ ).

Table 1 provides summary statistics describing the school-level analytical samples of Oregon elementary and middle school students in the three cohorts for mathematics and reading/language arts. Although variation existed from cohort to cohort in sample demographic characteristics, generally the composition of the samples was quite similar across the three cohorts and for mathematics and reading/language arts at each grade level band. From elementary to middle school cohorts, there were small but consistent decreases in the proportion of English learners (EL), economically disadvantaged students (EDS), racial/ethnic minority students (i.e., American Indian/Alaskan Native, Asian/Pacific Islander, Black/African American,

Hispanic, Multi-Ethnic, and Declined to report), and students with disabilities (SWD). At the elementary school level, almost $10 \%$ of the students were EL, almost $50 \%$ of the students were female, over $50 \%$ were EDS, approximately $33 \%$ were racial/ethnic minority students, and about $13 \%$ were SWD. It is also noteworthy that there was much greater school level variation-as indicated by the values of the standard deviations in parentheses-in EDS and racial/ethnic minority student school composition than other student characteristics. It should also be noted that when we refer to "school" composition, it references variables representing a particular cohort in each school in our analytic samples. Because we excluded students and schools to create our analytic samples, "total school" characteristics may differ slightly from the subsmaple characteristics reported here.

Table 1
Proportion and Standard Deviation (in parentheses) of Student Subgroups for the Oregon Analytical Samples by Content Area and Grade Level Band

|  |  | Cohort |  |  |
| :--- | :--- | ---: | ---: | ---: |
|  |  | 1 | 2 | 3 |
| Mathematics Elementary | EL | 0.102 | 0.097 | 0.093 |
|  |  | $(0.136)$ | $(0.129)$ | $(0.120)$ |
|  | Female | 0.495 | 0.496 | 0.496 |
|  |  | $(0.093)$ | $(0.086)$ | $(0.078)$ |
|  | EDS | 0.514 | 0.523 | 0.543 |
|  |  | $(0.262)$ | $(0.251)$ | $(0.247)$ |
|  | Ethnic | 0.323 | 0.332 | 0.343 |
|  | Minority | $(0.217)$ | $(0.218)$ | $(0.216)$ |
| Reading/Language Arts | SWD | 0.127 | 0.131 | 0.127 |
| Elementary | EL | $(0.065)$ | $(0.068)$ | $(0.063)$ |
|  |  | 0.093 | 0.096 | 0.093 |
|  | Female | $(0.121)$ | $(0.129)$ | $(0.119)$ |
|  |  | 0.497 | 0.497 | 0.497 |
|  | EDS | $(0.093)$ | $(0.087)$ | $(0.078)$ |
|  |  | 0.511 | 0.523 | 0.542 |
|  | Ethnic | $(0.262)$ | $(0.251)$ | $(0.247)$ |
|  | Minority | 0.316 | 0.333 | 0.344 |
|  | SWD | $(0.211)$ | $(0.218)$ | $(0.216)$ |
|  | 0.123 | 0.127 | 0.123 |  |
|  |  | $(0.064)$ | $(0.067)$ | $(0.062)$ |
| Mathematics Middle | 0.056 | 0.048 | 0.034 |  |
|  | EL | $(0.083)$ | $(0.067)$ | $(0.052)$ |
|  |  | 0.496 | 0.499 | 0.494 |
|  | Female | $(0.085)$ | $(0.091)$ | $(0.090)$ |


|  | EDS | 0.483 | 0.492 | 0.511 |
| :--- | :--- | ---: | ---: | ---: |
|  |  | $(0.237)$ | $(0.228)$ | $(0.227)$ |
|  | Ethnic | 0.307 | 0.321 | 0.330 |
|  | Minority | $(0.229)$ | $(0.220)$ | $(0.219)$ |
|  | SWD | 0.116 | 0.113 | 0.116 |
| Reading/Language Arts Middle | EL | $(0.065)$ | $(0.061)$ | $(0.068)$ |
|  |  | 0.056 | 0.047 | 0.033 |
|  | Female | $(0.083)$ | $(0.066)$ | $(0.050)$ |
|  |  | 0.495 | 0.500 | 0.494 |
|  | EDS | $(0.087)$ | $(0.092)$ | $(0.090)$ |
|  |  | 0.482 | 0.491 | 0.510 |
|  | Ethnic | $(0.238)$ | $(0.228)$ | $(0.227)$ |
|  | Minority | 0.307 | 0.319 | 0.330 |
|  | SWD | $(0.229)$ | $(0.220)$ | $(0.218)$ |
|  | 0.115 | 0.111 | 0.114 |  |
|  | $(0.065)$ | $(0.060)$ | $(0.066)$ |  |

## Instrument

The outcome measures for all analyses were the standardized Oregon Assessment of Knowledge and Skills (OAKS; Oregon Department of Education [ODE], 2012a) mathematics and reading/language arts tests. The OAKS is a summative, computer-adaptive assessment based on the Oregon content standards (ODE, 2008). OAKS test specifications varied by grade and content area and were intended to measure the core content standards in the state curriculum (ODE, 2012a). The tests were administered under standardized conditions (ODE, 2012b). OAKS raw scores were converted to scale scores based on the number of items answered correctly while taking item difficulty into account using one parameter item response theory (IRT) methods and a vertical linking design over grades to create a developmental scale score (ODE, 2009).

## Results and Discussion

This technical report is organized in three sections: Section A describes school performance model estimates, Section B describes school ranks, and the Appendices provide additional detailed results.

## Section A: School Performance Estimates

Cohort stability. We first considered the stability of model estimates by computing the correlations among estimates across the three successive cohorts of students. It should be noted that cohort comparisons are both an indication of changes in the composition of students in the school from one academic year to another as well as any other temporal changes that occur from one year to another including changes in policy, practice, instruction, or other factors that impact student test scores. Table 2 shows the correlation of model estimates across cohorts for mathematics and reading/language arts in the elementary school and middle school samples. As can be seen in Table 2, correlations generally ranged only from small to moderate for the model
estimates (with the exception of the MLM0 estimates) indicating some substantial instability in school performance estimates across cohorts. Correlations between adjacent years in the first two columns (cohort 1 with 2 or 2 with 3 ) are generally somewhat higher than the comparisons across two years (cohort 1 with 3 ). Although there is also some variation from elementary to middle school or from mathematics to reading/language arts, trends in cohort stability were fairly Table 2

Correlations of School Performance Model Estimates across Cohorts by Content Area and Grade Level Band

## Elementary Schools

|  | Mathematics |  |  |  | Reading/Language Arts |  |  |
| ---: | ---: | ---: | ---: | :--- | :--- | :--- | :--- |
| Model | 1 with 2 | 2 with 3 | 1 with 3 | 1 with 2 | 2 with 3 | 1 with 3 |  |
| PP | 0.593 | 0.630 | 0.529 | 0.655 | 0.667 | 0.593 |  |
| MLM0 | 0.782 | 0.815 | 0.732 | 0.823 | 0.829 | 0.797 |  |
| Gain | 0.369 | 0.305 | 0.174 | 0.281 | 0.261 | 0.084 |  |
| TM | 0.319 | 0.267 | 0.139 | 0.208 | 0.093 | 0.115 |  |
| SGP | 0.416 | 0.432 | 0.237 | 0.364 | 0.279 | 0.204 |  |
| VAM | 0.443 | 0.468 | 0.275 | 0.396 | 0.312 | 0.215 |  |
| Grate | 0.325 | 0.241 | 0.145 | 0.211 | 0.123 | 0.113 |  |
| AvGrate | 0.432 | 0.523 | 0.261 | 0.420 | 0.397 | 0.272 |  |

Middle Schools
Mathematics $\quad$ Reading/Language Arts

| Model | 1 with 2 | 2 with 3 | 1 with 3 | 1 with 2 | 2 with 3 | 1 with 3 |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PP | 0.713 | 0.670 | 0.586 | 0.674 | 0.668 | 0.672 |
| MLM0 | 0.823 | 0.788 | 0.770 | 0.848 | 0.812 | 0.840 |
| Gain | 0.300 | 0.299 | 0.212 | 0.294 | 0.255 | 0.246 |
| TM | 0.321 | 0.259 | 0.205 | 0.131 | -0.006 | 0.090 |
| SGP | 0.399 | 0.429 | 0.221 | 0.338 | 0.176 | 0.153 |
| VAM | 0.414 | 0.491 | 0.269 | 0.308 | 0.314 | 0.171 |
| Grate | 0.233 | 0.228 | 0.211 | 0.282 | 0.376 | 0.368 |


| AvGrate | 0.440 | 0.550 | 0.237 | 0.542 | 0.465 | 0.248 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

similar across content area and grade level band. To facilitate interpretation of the cohort results, we also averaged correlations across the two content areas and grade levels (see Table 3). It can be seen that the correlations across cohorts were largest for the two status based school performance measures (PP and MLM0) and noticeably lower for all other models that used two or three years of data to estimate school performance. The two rightmost columns of Table 3 show the overall mean and standard deviation across the cohort comparisons for each school performance model. It can be seen that the greatest agreement over cohorts, content, and grade level was for the MLM0 estimates (MLM focal year intercepts), closely followed by the PP model estimates. All remaining multi-year performance models had much greater instability. The standard deviations of correlations across cohort comparisons shown in the rightmost column of Table 3 also show the least variability over cohorts for the status models and the greatest variability across cohort correlations for the Average Growth Rate (AvGrate) model followed by the SGP model.

Table 3
Average Correlations across Content Area and Grade Level Band and Overall Mean and Standard Deviation (SD) Across the Three Cohort Comparisons

|  | 1 with | 2 with | 1 with |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: |
| Model | 2 | 3 | 3 | Mean | SD |
| PP | 0.659 | 0.659 | 0.595 | 0.638 | 0.040 |
| MLM0 | 0.819 | 0.811 | 0.785 | 0.805 | 0.026 |
| Gain | 0.311 | 0.280 | 0.179 | 0.257 | 0.071 |
| TM | 0.245 | 0.153 | 0.137 | 0.178 | 0.071 |
| SGP | 0.379 | 0.329 | 0.204 | 0.304 | 0.100 |
| VAM | 0.390 | 0.396 | 0.232 | 0.339 | 0.097 |
| Grate | 0.263 | 0.242 | 0.209 | 0.238 | 0.052 |
| AvGrate | 0.458 | 0.484 | 0.254 | 0.399 | 0.131 |
| Mean | 0.440 | 0.419 | 0.324 | -- | -- |

Comparison of models. We next computed the correlations of school performance estimates from one model to another within each of the three cohorts and then took the mean correlation across cohorts. Correlations of model estimates within each individual cohort are presented in Appendix A. Table 4 shows model correlations for mathematics and reading/language arts in the elementary school and middle school samples averaged over the three cohorts.

Table 4
Correlations of School Performance Estimates across Models by Content Area and Grade Level Band and Averaged over Content and Grade Band

Elementary School Mathematics

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: |
| PP | 0.826 | 0.260 | 0.358 | 0.495 | 0.516 | 0.169 | 0.383 |
| MLM0 |  | 0.276 | 0.316 | 0.55 | 0.592 | 0.179 | 0.426 |
| Gain |  |  | 0.894 | 0.849 | 0.872 | 0.960 | 0.573 |
| TM |  |  |  | 0.812 | 0.814 | 0.843 | 0.549 |
| SGP |  |  |  |  | 0.957 | 0.717 | 0.803 |
| VAM |  |  |  |  |  | 0.736 | 0.843 |
| Grate |  |  |  |  |  |  | 0.347 |

Elementary School Reading/Language Arts

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | 0.844 | -0.015 | 0.260 | 0.448 | 0.519 | -0.013 | -0.044 |
| MLM0 |  | -0.107 | 0.196 | 0.445 | 0.511 | -0.120 | -0.136 |
| Gain |  |  | 0.423 | 0.481 | 0.499 | 0.442 | 0.555 |
| TM |  |  |  | 0.709 | 0.716 | 0.672 | 0.406 |
| SGP |  |  |  |  | 0.913 | 0.535 | 0.587 |
| VAM |  |  |  |  |  | 0.576 | 0.629 |
| Grate |  |  |  |  |  |  | 0.274 |

Middle School Mathematics

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: |
| PP | 0.785 | 0.456 | 0.572 | 0.513 | 0.508 | 0.431 | 0.381 |
| MLM0 |  | 0.467 | 0.471 | 0.512 | 0.547 | 0.479 | 0.372 |
| Gain |  |  | 0.887 | 0.88 | 0.909 | 0.952 | 0.643 |
| TM |  |  |  | 0.811 | 0.809 | 0.836 | 0.577 |
| SGP |  |  |  |  | 0.948 | 0.762 | 0.840 |


| VAM | 0.803 | 0.884 |
| :--- | :--- | :--- |
| Grate |  | 0.448 |

Middle School Reading/Language Arts

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | 0.853 | -0.139 | 0.360 | 0.395 | 0.399 | -0.308 | -0.143 |
| MLM0 |  | -0.296 | 0.226 | 0.342 | 0.368 | -0.438 | -0.250 |
| Gain |  |  | 0.678 | 0.661 | 0.675 | 0.916 | 0.602 |
| TM |  |  |  | 0.732 | 0.719 | 0.527 | 0.384 |
| SGP |  |  |  |  | 0.897 | 0.437 | 0.598 |
| VAM |  |  |  |  |  | 0.499 | 0.682 |
| Grate |  |  |  |  |  |  | 0.452 |

Average over Content Area and Grade Level Band

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | 0.827 | 0.141 | 0.388 | 0.463 | 0.486 | 0.070 | 0.144 |
| MLM0 |  | 0.085 | 0.302 | 0.462 | 0.505 | 0.025 | 0.103 |
| Gain |  |  | 0.721 | 0.718 | 0.739 | 0.818 | 0.593 |
| TM |  |  |  | 0.766 | 0.765 | 0.720 | 0.479 |
| SGP |  |  |  |  | 0.929 | 0.613 | 0.707 |
| VAM |  |  |  |  |  | 0.654 | 0.760 |
| Grate |  |  |  |  |  |  | 0.380 |

As can be seen in Table 4, substantial variability was present in the degree to which school performance estimates for one model were related to other models and the correlations among models varied a good deal depending on content area and grade level band. For example, the correlation between the PP model and the Gain score model ranged from -. 139 to +.456 and between MLM0 and MLM Grate ranged from -.438 to +.479 . The least variation in model correlations across content area and grade level band was for the SGP and VAM models from +.897 to +.957 .

As shown in the last panel of Table 4, on average across content area and grade level band, the highest correlations were among the SGP and VAM models (+.929), the PP and

MLM0 models (+.827), and the Gain score model with the Grate model (+.818). The lowest correlations were between the MLM intercept (MLM0) and MLM growth rate (Grate) models (+.025), the MLM0 model and the Gain model (+.085), and the MLM0 and the average growth rate (AvGrate) model (+.103). The average correlation of the two status models (PP, MLM0) with the remaining six multiyear models was only +.264 . Average correlations among the six multiple year models ranged from +.479 to +.766 with one exception, the correlation of the Grate and AvGrate models was only +.380 , with an average correlation among all six multiyear models of +.691 .

We also examined the degree to which school performance model estimates were consistent from one content area to the other. Table 5 shows model estimate agreement across content areas in each cohort as well as the average across the three cohorts. As can be seen in Table 5, correlations were higher between content areas in elementary than middle school. On average, correlations for the two status models (PP and MLM0) were greater than +.70 and higher than average correlations for the other models that ranged from +.183 to +.578 .

Table 5
Correlations of School Performance Model Estimates between Mathematics and Reading/Language Arts by Grade Level Band in each Cohort and Averaged over Cohorts

| Elementary Schools |  |  |  |  |  | Middle Schools |  |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Cohort |  |  |  | Mean | 1 | 2 | 3 |  |
| Model | 1 | 2 | 3 | Mean |  |  |  |  |  |
| PP | 0.772 | 0.753 | 0.761 | 0.762 | 0.725 | 0.720 | 0.702 | 0.716 |  |
| MLM0 | 0.865 | 0.852 | 0.845 | 0.854 | 0.819 | 0.773 | 0.775 | 0.789 |  |
| Gain | 0.563 | 0.508 | -0.122 | 0.316 | 0.261 | 0.326 | 0.281 | 0.289 |  |
| TM | 0.454 | 0.448 | 0.390 | 0.431 | 0.217 | 0.370 | 0.304 | 0.297 |  |
| SGP | 0.558 | 0.503 | 0.513 | 0.525 | 0.417 | 0.401 | 0.373 | 0.397 |  |
| VAM | 0.585 | 0.585 | 0.565 | 0.578 | 0.439 | 0.356 | 0.473 | 0.423 |  |
| Grate | 0.582 | 0.468 | 0.385 | 0.478 | 0.188 | 0.215 | 0.145 | 0.183 |  |
| AvGrate | 0.539 | 0.593 | 0.511 | 0.548 | 0.407 | 0.434 | 0.452 | 0.431 |  |

Relation with school composition variables. We computed the correlation of model estimates with school composition variables to determine whether estimates were related to the aggregated student characteristics in each school. Table 6 shows the correlations of model estimates with school composition variables for mathematics and reading/language arts in the elementary school and middle school samples. Correlations of model estimates with school composition variables within each individual cohort are presented in Appendix B.

The rightmost column of Table 6 shows the average correlation of each school performance model with the school composition variables across all school composition variables. As can be seen, correlations of the status models, PP and MLM0, were negative and noticeably higher than the correlations of the other school performance models with school
composition variables. On average across content and grade level band, the correlation of the school composition variables was -0.221 for the PP model and -0.225 for the MLM0 model. In contrast, the average correlations of the school composition variables with the remaining models were quite low ranging from -0.003 to +0.117 . Thus there was relatively little relation of the multiyear models with school composition, but for the status models performance estimates were higher the fewer the number of students from protected groups present in the school and lower as the number of students from protected groups increased. No clear pattern was present for the relation between school size and model estimates.

Table 6
Correlations of Model Estimates with School Composition Variables by Content Area and Grade Level Band

Elementary School Mathematics

|  |  |  |  |  | Ethnic |  | School |  |
| ---: | :--- | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |  |
| PP | -0.500 | -0.328 | -0.194 | 0.013 | -0.319 | 0.147 | -0.197 |  |
| MLM0 | -0.626 | -0.339 | -0.195 | -0.012 | -0.299 | 0.228 | -0.207 |  |
| Gain | -0.016 | 0.052 | 0.017 | -0.003 | 0.021 | 0.099 | 0.028 |  |
| TM | -0.058 | 0.031 | -0.016 | -0.006 | -0.011 | 0.097 | 0.006 |  |
| SGP | -0.158 | -0.016 | -0.036 | -0.009 | -0.028 | 0.171 | -0.013 |  |
| VAM | -0.180 | -0.024 | -0.052 | 0.006 | -0.035 | 0.187 | -0.016 |  |
| Grate | -0.013 | 0.032 | 0.029 | -0.006 | -0.003 | 0.062 | 0.017 |  |
| AvGrate | -0.020 | 0.090 | -0.028 | 0.027 | 0.083 | 0.170 | 0.053 |  |

Elementary School Reading/Language Arts

|  |  |  |  |  | Ethnic |  | School |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |  |
| PP | -0.600 | -0.526 | -0.204 | 0.002 | -0.492 | 0.064 | -0.293 |  |
| MLM0 | -0.725 | -0.526 | -0.189 | 0.001 | -0.477 | 0.132 | -0.297 |  |
| Gain | 0.158 | 0.184 | 0.076 | -0.024 | 0.117 | 0.067 | 0.096 |  |
| TM | -0.072 | 0.051 | 0.035 | 0.002 | 0.008 | 0.084 | 0.018 |  |
| SGP | -0.210 | -0.061 | -0.041 | -0.003 | -0.105 | 0.110 | -0.052 |  |
| VAM | -0.259 | -0.110 | -0.059 | 0.009 | -0.141 | 0.125 | -0.072 |  |
| Grate | 0.142 | 0.130 | 0.054 | 0.023 | 0.090 | 0.005 | 0.074 |  |
| AvGrate | 0.237 | 0.285 | 0.057 | -0.002 | 0.210 | 0.052 | 0.140 |  |

Middle School Mathematics
EDS EL SWD Female Ethnic School Mean

| Model |  |  |  | Minority |  |  | Size |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.329 | -0.229 | -0.267 | 0.051 | -0.265 | 0.169 | -0.145 |  |
| MLM0 | -0.466 | -0.232 | -0.179 | 0.009 | -0.184 | 0.236 | -0.136 |  |
| Gain | -0.009 | 0.017 | -0.070 | 0.030 | 0.056 | 0.140 | 0.027 |  |
| TM | -0.046 | -0.001 | -0.118 | 0.037 | 0.005 | 0.166 | 0.007 |  |
| SGP | 0.005 | 0.045 | -0.049 | 0.026 | 0.060 | 0.172 | 0.043 |  |
| VAM | 0.006 | 0.045 | -0.048 | 0.020 | 0.063 | 0.181 | 0.044 |  |
| Grate | -0.090 | -0.045 | -0.074 | 0.011 | -0.001 | 0.138 | -0.010 |  |
| AvGrate | 0.134 | 0.128 | 0.001 | 0.020 | 0.113 | 0.150 | 0.091 |  |

Middle School Reading/Language Arts

|  |  |  |  |  | Ethnic |  | School |  |
| ---: | :---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |  |
| PP | -0.525 | -0.444 | -0.263 | 0.135 | -0.481 | 0.088 | -0.248 |  |
| MLM0 | -0.663 | -0.459 | -0.217 | 0.120 | -0.456 | 0.109 | -0.261 |  |
| Gain | 0.326 | 0.238 | 0.092 | -0.026 | 0.226 | 0.031 | 0.148 |  |
| TM | -0.021 | 0.001 | -0.001 | 0.036 | -0.028 | 0.112 | 0.017 |  |
| SGP | -0.063 | 0.016 | -0.035 | 0.056 | -0.047 | 0.128 | 0.009 |  |
| VAM | -0.058 | 0.002 | -0.038 | 0.041 | -0.058 | 0.121 | 0.002 |  |
| Grate | 0.365 | 0.256 | 0.126 | -0.054 | 0.235 | 0.007 | 0.156 |  |
| AvGrate | 0.394 | 0.339 | 0.098 | -0.039 | 0.258 | 0.057 | 0.185 |  |

Relation of Model Estimates to SWD School Composition. Because of the NCAASE emphasis on the performance and academic growth of SWD, we also focused more specifically on the relations between the percentage of SWD students served by a school and the school performance model estimates. Correlations of model estimates with SWD school composition within each individual cohort are presented in Appendix C. Table 7 shows the correlation of model estimates with the percentage of SWD in each school for mathematics and reading/language arts in the elementary school and middle school samples averaged over cohorts. As can be seen in the bottom row of Table 7, average school performance estimates based on the single-year, status models (PP and MLM0) had substantially higher correlations with school SWD composition than the other school performance models. With the PP and MLM0 models, school performance estimates were higher the lower the percentage of SWD students in the school and lower to the extent that the school served higher proportions of SWD.

Table 7
Average School Performance Model Estimates as a Function of the Percentage of SWD in the School by Content Area and Grade Level Band

| Content Area and |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Grade Level Band | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |


| Math Elementary | -0.194 | -0.195 | 0.017 | -0.016 | -0.036 | -0.052 | 0.029 | -0.028 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Math Middle | -0.204 | -0.189 | 0.076 | 0.035 | -0.041 | -0.059 | 0.054 | 0.057 |
| Reading/Language <br> Arts Elementary | -0.267 | -0.179 | -0.070 | -0.118 | -0.049 | -0.048 | -0.074 | 0.001 |
| Reading/Language <br> Arts Middle | -0.263 | -0.217 | 0.092 | -0.001 | -0.035 | -0.038 | 0.126 | 0.098 |
| Mean | -0.232 | -0.195 | 0.029 | -0.025 | -0.040 | -0.049 | 0.034 | 0.032 |

Summary of Section A. We evaluated eight alternative models for estimating school academic performance in mathematics and reading/language arts using operational Oregon state accountability data. We observed substantial variability in model estimates across three successive student cohorts in mathematics and reading/language arts in both elementary and middle school grades. Variability across cohorts was somewhat less for the two status models (PP and MLM0) than for the remaining models that used more than one year of data. We also compared the estimates of school performance from one model to another and found substantial disagreement across models. Generally, the status models based on a single year of data were more similar to each other and differed from the remaining models that examined more than one year of data. There was greater agreement among the models that used multiple years of data. We also compared school performance estimates in mathematics with those in reading/language arts. Again, agreement was greater across content areas for the status models than for the multiple year models. Comparison of model estimates with school composition variables showed that status models (PP and MLM0) had substantially higher correlations than the remaining school performance models with the student makeup of the school with lower estimates related to higher proportions of protected student subgroups in the school. Finally, we correlated school performance estimates with the percentage of SWD in each school. Ideally estimates of school performance should be unrelated to the student composition of the school, but as with the other school composition variables, we found that the status models were more highly correlated with SWD school composition and there were noticeably lower correlations of the multiyear model estimates with the percentage of SWD students in the school.

## Section B: School Ranks Based on School Performance Estimates

The purpose of Section B of this technical report is to describe study results based on school ranks. In section A, we focused on the examination of school performance estimates that arose from the eight school performance models. In section B, we focus on the examination of school ranks based on those school performance estimates. The methods for analyzing school ranks, comparing school ranks across cohorts, and comparing school performance models using school ranks were described above in the General Methods section. Common practice for states and other jurisdictions is to rank schools as a method for evaluating academic performance. Therefore, using the estimates of school performance generated by the eight models described previously, we computed percentile ranks for each school. We then compared school ranks within each school performance model across the three cohorts used in the study. Next we compared the school ranks for each model to the ranks obtained from each of the other models. Finally we examined the relation between school ranks from each model with variables describing the student composition of each school. Three criteria were used to evaluate the
comparisons of school ranks: (a) the Spearman's correlation between school ranks, (b) the proximity of absolute school ranks, and (c) the root mean square difference (RMSD) in school ranks.

Comparison of cohorts. We first consider the stability of school ranks within each school performance model across the three successive cohorts of students in mathematics and reading/language arts in the elementary and middle school grades. We computed the Spearman's correlation of the school ranks from one cohort to the school ranks from each of the other two cohorts within each of the eight school performance models to determine the stability of school ranks. As mentioned in Section A, cohort comparisons are both an indication of changes in the composition of students in the school from one academic year to another as well as any other temporal changes that occur from one year to another including changes in policy, practice, instruction, or other factors that impact student test scores. Table 8 shows the correlation of school ranks across cohorts for mathematics and reading/language arts in the elementary school and middle school samples. As can be seen in Table 8, the correlations generally ranged from small to moderate indicating substantial variability in school ranks from one cohort to another. As would be expected, correlations between adjacent years in the first two columns (cohort 1 with 2 or 2 with 3 ) were generally somewhat higher than the comparison across two years (cohort 1 with 3). Although there was some variation, results were quite similar from elementary to middle school or from mathematics to reading/language arts.

Table 8
Spearman's Correlations of Model School Ranks for Each Pair of Cohorts by Content Area and Grade Level Band

## Elementary Schools

|  | Mathematics |  |  |  | Reading/Language Arts |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | 1 with 2 | 2 with 3 | 1 with 3 | 1 with 2 | 2 with 3 | 1 with 3 |  |
| PP | 0.620 | 0.613 | 0.529 | 0.658 | 0.659 | 0.609 |  |
| MLM0 | 0.748 | 0.787 | 0.693 | 0.812 | 0.811 | 0.787 |  |
| Gain | 0.349 | 0.262 | 0.141 | 0.240 | 0.247 | 0.070 |  |
| TM | 0.315 | 0.255 | 0.117 | 0.173 | 0.116 | 0.102 |  |
| SGP | 0.406 | 0.409 | 0.217 | 0.354 | 0.282 | 0.193 |  |
| VAM | 0.428 | 0.450 | 0.235 | 0.388 | 0.324 | 0.215 |  |
| Grate | 0.297 | 0.195 | 0.124 | 0.195 | 0.120 | 0.120 |  |
| AvGrate | 0.419 | 0.512 | 0.242 | 0.424 | 0.384 | 0.248 |  |

## Middle Schools

|  | Mathematics |  |  |  | Reading/Language Arts |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | 1 with 2 | 2 with 3 | 1 with 3 | 1 with 2 | 2 with 3 | 1 with 3 |  |
| PP | 0.675 | 0.635 | 0.511 | 0.707 | 0.686 | 0.684 |  |
| MLM0 | 0.754 | 0.730 | 0.700 | 0.837 | 0.797 | 0.824 |  |
| Gain | 0.269 | 0.267 | 0.167 | 0.263 | 0.304 | 0.281 |  |
| TM | 0.306 | 0.222 | 0.171 | 0.096 | 0.121 | 0.086 |  |
| SGP | 0.373 | 0.418 | 0.197 | 0.323 | 0.243 | 0.162 |  |
| VAM | 0.402 | 0.452 | 0.238 | 0.295 | 0.301 | 0.158 |  |
| Grate | 0.230 | 0.207 | 0.169 | 0.272 | 0.370 | 0.373 |  |
| AvGrate | 0.442 | 0.512 | 0.201 | 0.516 | 0.456 | 0.261 |  |

To facilitate further interpretation, we averaged the results shown in Table 8 across content area and grade level band. As can be seen in Table 9, on average the greatest stability was for the two status models, PP and MLM0. Noticeably lower correlations occurred for the remaining school performance models, all of which were based on more than one year of data, with the least stability for the TM, Grate, and Gain models.

Table 9
Spearman's Correlations of Model School Ranks Averaged across Content Area and Grade Level Band and Overall Mean and Standard Deviation (SD) Across the Three Cohort Comparisons

|  | 1 with | 2 with | 1 with |  |  |
| ---: | ---: | ---: | ---: | :--- | :---: |
| Model | 2 | 3 | 3 | Mean | SD |
| PP | 0.665 | 0.648 | 0.583 | 0.632 | 0.044 |
| MLM0 | 0.788 | 0.781 | 0.751 | 0.773 | 0.027 |
| Gain | 0.280 | 0.270 | 0.165 | 0.238 | 0.071 |
| TM | 0.222 | 0.178 | 0.119 | 0.173 | 0.056 |
| SGP | 0.364 | 0.338 | 0.192 | 0.298 | 0.097 |
| VAM | 0.378 | 0.382 | 0.212 | 0.324 | 0.100 |
| Grate | 0.248 | 0.223 | 0.196 | 0.222 | 0.055 |
| AvGrate | 0.450 | 0.466 | 0.238 | 0.385 | 0.131 |

Our second criterion for comparing school ranks was to determine how much a school's rank changed from one cohort to another. Table 10 shows the proportion of schools that were within 5,10 , or 20 ranks in one cohort versus another for each school performance model in mathematics and reading/language arts at each grade level band. The last table entry for each school performance model shows the average differences in school ranks averaged over content area and grade level band. It can be seen that on average for the PP model, about one quarter of the schools differed by only 5 percentile ranks or less, slightly over $40 \%$ of schools differed by 10 ranks or less, and slightly more than $60 \%$ differed by 20 ranks or less. This also indicates that over a third of schools differed by more than 20 ranks from one cohort to another. The results for the MLM0 model showed slightly greater agreement in school ranks across cohorts.
However, the level of agreement in school ranks across cohorts was noticeably lower for all of the remaining models that were based on two or more years of achievement data. For example, school ranks based on the remaining models (Gain, TM, SGP, VAM, Grate, and AvGrate) differed by more than 20 ranks for about $50 \%$ or more of the schools.

Table 10
Proportion of Elementary or Middle Schools Within 5, 10, or 20 Ranks of Each Other for each School Performance Model for each Pair of Cohorts in Mathematics and Reading/Language Arts

PP

|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| :--- | :---: | :---: | :---: | :---: |
| Mathematics Elementary | 1 vs. 2 | 0.229 | 0.380 | 0.642 |
|  | 2 vs. 3 | 0.236 | 0.383 | 0.617 |
|  | 1 vs. 3 | 0.228 | 0.376 | 0.589 |
| Reading/Language Arts Elementary | 1 vs. 2 | 0.267 | 0.437 | 0.652 |
|  | 2 vs. 3 | 0.225 | 0.389 | 0.652 |
|  | 1 vs. 3 | 0.219 | 0.387 | 0.629 |
| Mathematics Middle | 1 vs. 2 | 0.255 | 0.420 | 0.646 |
|  | 2 vs. 3 | 0.272 | 0.399 | 0.638 |
| Reading/Language Arts Middle | 1 vs. 3 | 0.259 | 0.395 | 0.580 |
|  | 1 vs. 2 | 0.284 | 0.453 | 0.741 |
|  | 2 vs. 3 | 0.309 | 0.490 | 0.700 |
|  | 1 vs. 3 | 0.259 | 0.465 | 0.695 |
| Mean | 1 vs. 2 | 0.259 | 0.422 | 0.670 |
|  | 2 vs. 3 | 0.260 | 0.415 | 0.652 |
|  | 1 vs. 3 | 0.241 | 0.406 | 0.623 |

## MLM0

|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| :--- | :--- | :---: | :---: | :---: |
| Mathematics Elementary | 1 vs. 2 | 0.289 | 0.452 | 0.718 |
|  | 2 vs. 3 | 0.309 | 0.512 | 0.752 |
|  | 1 vs. 3 | 0.262 | 0.421 | 0.685 |
| Reading Elementary | 1 vs. 2 | 0.288 | 0.520 | 0.773 |
|  | 2 vs. 3 | 0.325 | 0.525 | 0.783 |
|  | 1 vs. 3 | 0.296 | 0.508 | 0.724 |
| Mathematics Middle | 1 vs. 2 | 0.292 | 0.481 | 0.691 |
|  | 2 vs. 3 | 0.267 | 0.436 | 0.695 |
| Reading Middle | 1 vs. 3 | 0.272 | 0.440 | 0.671 |
|  | 1 vs. 2 | 0.354 | 0.593 | 0.811 |
|  | 2 vs. 3 | 0.374 | 0.539 | 0.790 |
|  | 1 vs. 3 | 0.342 | 0.523 | 0.798 |
| Mean | 1 vs. 2 | 0.306 | 0.511 | 0.748 |
|  | 2 vs. 3 | 0.319 | 0.503 | 0.755 |
|  | 1 vs. 3 | 0.293 | 0.473 | 0.720 |

## Gain

|  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| Mathematics Elementary | 1 vs. 2 | 0.158 | 0.295 | 0.487 |
|  | 2 vs. 3 | 0.144 | 0.261 | 0.467 |
|  | 1 vs. 3 | 0.140 | 0.243 | 0.422 |
| Reading Elementary | 1 vs. 2 | 0.142 | 0.250 | 0.440 |
|  | 2 vs. 3 | 0.171 | 0.283 | 0.447 |
|  | 1 vs. 3 | 0.141 | 0.233 | 0.406 |
| Mathematics Middle | 1 vs. 2 | 0.165 | 0.284 | 0.453 |
|  | 2 vs. 3 | 0.148 | 0.267 | 0.486 |
|  | 1 vs. 3 | 0.119 | 0.235 | 0.412 |
| Reading Middle | 1 vs. 2 | 0.173 | 0.309 | 0.486 |
|  |  |  | 20 |  |


|  | 2 vs. 3 | 0.173 | 0.292 | 0.498 |
| :--- | :--- | :--- | :--- | :--- |
|  | 1 vs. 3 | 0.136 | 0.305 | 0.490 |
| Mean | 1 vs. 2 | 0.160 | 0.284 | 0.466 |
|  | 2 vs. 3 | 0.159 | 0.276 | 0.475 |
|  | 1 vs. 3 | 0.134 | 0.254 | 0.432 |

TM

|  |  |  |  |  |
| :--- | :--- | :---: | :---: | :---: |
|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| Mathematics Elementary | 1 vs. 2 | 0.155 | 0.276 | 0.500 |
|  | 2 vs. 3 | 0.144 | 0.248 | 0.459 |
|  | 1 vs. 3 | 0.127 | 0.249 | 0.452 |
| Reading Elementary | 1 vs. 2 | 0.131 | 0.233 | 0.445 |
|  | 2 vs. 3 | 0.123 | 0.235 | 0.440 |
|  | 1 vs. 3 | 0.118 | 0.212 | 0.394 |
| Mathematics Middle | 1 vs. 2 | 0.152 | 0.280 | 0.494 |
|  | 2 vs. 3 | 0.165 | 0.276 | 0.490 |
|  | 1 vs. 3 | 0.165 | 0.247 | 0.432 |
| Reading Middle | 1 vs. 2 | 0.128 | 0.243 | 0.432 |
|  | 2 vs. 3 | 0.132 | 0.247 | 0.477 |
|  | 1 vs. 3 | 0.128 | 0.235 | 0.383 |
| Mean | 1 vs. 2 | 0.142 | 0.258 | 0.468 |
|  | 2 vs. 3 | 0.141 | 0.252 | 0.466 |
|  | 1 vs. 3 | 0.134 | 0.236 | 0.415 |

## SGP

|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| :--- | :---: | :---: | :---: | :---: |
| Mathematics Elementary | 1 vs. 2 | 0.168 | 0.285 | 0.495 |
|  | 2 vs. 3 | 0.191 | 0.299 | 0.500 |
|  | 1 vs. 3 | 0.150 | 0.256 | 0.446 |
| Reading Elementary | 1 vs. 2 | 0.179 | 0.278 | 0.490 |
|  |  |  | 21 |  |


|  | 2 vs. 3 | 0.149 | 0.273 | 0.480 |
| :--- | :--- | :--- | :--- | :--- |
|  | 1 vs. 3 | 0.151 | 0.243 | 0.424 |
| Mathematics Middle | 1 vs. 2 | 0.206 | 0.321 | 0.502 |
|  | 2 vs. 3 | 0.156 | 0.313 | 0.568 |
| Reading Middle | 1 vs. 3 | 0.177 | 0.259 | 0.420 |
|  | 1 vs. 2 | 0.169 | 0.305 | 0.481 |
|  | 2 vs. 3 | 0.132 | 0.272 | 0.490 |
|  | 1 vs. 3 | 0.119 | 0.276 | 0.395 |
| Mean | 1 vs. 2 | 0.180 | 0.297 | 0.492 |
|  | 2 vs. 3 | 0.157 | 0.289 | 0.509 |
|  | 1 vs. 3 | 0.149 | 0.258 | 0.421 |

VAM

|  |  |  |  |  |
| :--- | :--- | :---: | :---: | :---: |
| Mathematics Elementary | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
|  | 2 vs. 2 | 0.172 | 0.305 | 0.508 |
| Reading Elementary | 0.168 | 0.305 | 0.520 |  |
|  | 1 vs. 3 | 0.147 | 0.243 | 0.444 |
|  | 1 vs. 2 | 0.159 | 0.262 | 0.498 |
|  | 2 vs. 3 | 0.159 | 0.280 | 0.480 |
| Mathematics Middle | 1 vs. 3 | 0.131 | 0.230 | 0.419 |
|  | 1 vs. 2 | 0.198 | 0.309 | 0.510 |
| Reading Middle | 2 vs. 3 | 0.218 | 0.325 | 0.510 |
|  | 1 vs. 3 | 0.140 | 0.243 | 0.449 |
|  | 1 vs. 2 | 0.169 | 0.276 | 0.469 |
|  | 2 vs. 3 | 0.152 | 0.263 | 0.473 |
|  | 1 vs. 3 | 0.169 | 0.251 | 0.395 |
| Mean | 1 vs. 2 | 0.174 | 0.288 | 0.496 |
|  | 2 vs. 3 | 0.174 | 0.293 | 0.496 |
|  | 1 vs. 3 | 0.147 | 0.242 | 0.427 |

## Grate

|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| :--- | :--- | :---: | :---: | :---: |
| Mathematics Elementary | 1 vs. 2 | 0.168 | 0.272 | 0.467 |
|  | 2 vs. 3 | 0.145 | 0.257 | 0.452 |
|  | 1 vs. 3 | 0.117 | 0.231 | 0.394 |
| Reading Elementary | 1 vs. 2 | 0.139 | 0.255 | 0.442 |
|  | 2 vs. 3 | 0.121 | 0.224 | 0.389 |
| Mathematics Middle | 1 vs. 3 | 0.137 | 0.240 | 0.417 |
|  | 1 vs. 2 | 0.144 | 0.247 | 0.465 |
| Reading Middle | 2 vs. 3 | 0.169 | 0.280 | 0.420 |
|  | 1 vs. 3 | 0.132 | 0.259 | 0.416 |
|  | 1 vs. 2 | 0.181 | 0.296 | 0.502 |
|  | 2 vs. 3 | 0.165 | 0.305 | 0.531 |
|  | 1 vs. 3 | 0.152 | 0.313 | 0.473 |
| Mean | 1 vs. 2 | 0.158 | 0.268 | 0.469 |
|  | 2 vs. 3 | 0.150 | 0.266 | 0.448 |
|  | 1 vs. 3 | 0.134 | 0.261 | 0.425 |

AvGrate

|  | Cohort | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| :--- | :--- | :--- | :--- | :--- |
| Mathematics Elementary | 1 vs. 2 | 0.147 | 0.271 | 0.507 |
|  | 2 vs. 3 | 0.173 | 0.325 | 0.561 |
|  | 1 vs. 3 | 0.145 | 0.254 | 0.457 |
| Reading Elementary | 1 vs. 2 | 0.172 | 0.295 | 0.517 |
|  | 2 vs. 3 | 0.137 | 0.265 | 0.470 |
| Mathematics Middle | 1 vs. 3 | 0.154 | 0.255 | 0.444 |
|  | 1 vs. 2 | 0.169 | 0.313 | 0.490 |
| Reading Middle | 2 vs. 3 | 0.206 | 0.317 | 0.543 |
|  | 1 vs. 3 | 0.115 | 0.222 | 0.370 |
|  | 1 vs. 2 | 0.198 | 0.342 | 0.568 |
|  | 2 vs. 3 | 0.165 | 0.296 | 0.539 |


|  | 1 vs. 3 | 0.136 | 0.280 | 0.490 |
| :--- | :--- | :--- | :--- | :--- |
| Mean | 1 vs. 2 | 0.172 | 0.305 | 0.520 |
|  | 2 vs. 3 | 0.170 | 0.301 | 0.528 |
|  | 1 vs. 3 | 0.138 | 0.253 | 0.440 |

Our third criterion for comparing school ranks was to calculate the root mean square difference (RMSD) between cohorts or models as defined above in the General Method section. Table 11 shows the RMSD across pairs of cohorts by content area and grade level band for each of the eight school performance models and in the last two columns the mean and standard deviation (SD) across cohort comparisons. As can be seen in the table, the smallest differences in rank were for the MLM0 model, about 17 to 21 ranks on average, followed by the PP model. Average differences in school rank across cohorts for the remaining models ranged from about 31 to 38 .

Table 11
RMSD in School Ranks for each Student Cohort for each School Performance Model by Content Area and Grade Level Band

Elementary School Mathematics

| Model | 1 with 2 | 2 with 3 | 1 with 3 | Mean | SD |
| ---: | ---: | ---: | ---: | :--- | :---: |
| PP | 24.884 | 25.134 | 27.684 | 25.901 | 1.549 |
| MLM0 | 20.269 | 18.610 | 22.355 | 20.411 | 1.877 |
| Gain | 32.555 | 34.659 | 37.401 | 34.872 | 2.430 |
| TM | 33.382 | 34.818 | 37.929 | 35.376 | 2.324 |
| SGP | 31.076 | 31.011 | 35.696 | 32.594 | 2.686 |
| VAM | 30.527 | 29.940 | 35.304 | 31.924 | 2.942 |
| Grate | 33.823 | 36.204 | 37.772 | 35.933 | 1.988 |
| AvGrate | 30.753 | 28.179 | 35.139 | 31.357 | 3.519 |

Elementary School Reading/Language Arts

| Model | 1 with 2 | 2 with 3 | 1 with 3 | Mean | SD |
| ---: | :---: | ---: | ---: | :---: | :---: |
| PP | 23.598 | 23.592 | 25.257 | 24.149 | 0.960 |
| MLM0 | 17.507 | 17.542 | 18.631 | 17.893 | 0.639 |
| Gain | 35.183 | 35.019 | 38.914 | 36.372 | 2.203 |
| TM | 36.703 | 37.928 | 38.240 | 37.624 | 0.812 |
| SGP | 32.430 | 34.189 | 36.250 | 34.290 | 1.912 |
| VAM | 31.568 | 33.183 | 35.764 | 33.505 | 2.116 |
| Grate | 36.207 | 37.847 | 37.852 | 37.302 | 0.948 |
| AvGrate | 30.618 | 31.678 | 35.001 | 32.432 | 2.287 |

Middle School Mathematics

| Model | 1 with 2 | 2 with 3 | 1 with 3 | Mean | SD |
| ---: | ---: | ---: | ---: | :---: | :---: |
| PP | 22.959 | 24.334 | 28.150 | 25.148 | 2.689 |
| MLM0 | 19.945 | 20.889 | 22.024 | 20.953 | 1.041 |
| Gain | 34.406 | 34.469 | 36.731 | 35.202 | 1.325 |
| TM | 33.549 | 35.508 | 36.662 | 35.240 | 1.574 |
| SGP | 31.858 | 30.695 | 36.080 | 32.878 | 2.834 |
| VAM | 31.125 | 29.782 | 35.122 | 32.010 | 2.778 |
| Grate | 35.309 | 35.846 | 36.690 | 35.948 | 0.696 |
| AvGrate | 30.048 | 28.129 | 35.970 | 31.382 | 4.087 |

Middle School Reading/Language Arts

| Model | 1 with 2 | 2 with 3 | 1 with 3 | Mean | SD |
| ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 21.787 | 22.540 | 22.604 | 22.310 | 0.454 |
| MLM0 | 16.271 | 18.141 | 16.903 | 17.105 | 0.951 |
| Gain | 34.532 | 33.582 | 34.127 | 34.080 | 0.477 |
| TM | 38.265 | 37.749 | 38.471 | 38.162 | 0.372 |
| SGP | 33.096 | 35.016 | 36.844 | 34.985 | 1.874 |
| VAM | 33.787 | 33.661 | 36.927 | 34.792 | 1.851 |
| Grate | 34.337 | 31.956 | 31.883 | 32.725 | 1.396 |
| AvGrate | 28.016 | 29.695 | 34.590 | 30.767 | 3.416 |

Comparison of models. We next compared school ranks from one model to another within each of the three cohorts. Comparisons of school ranks within each individual cohort were computed and are presented in Appendix D. We averaged those results by taking the median absolute difference in school ranks over the three cohorts in mathematics and reading/language arts in the elementary and middle school grades. For each pair of school performance models, Table 12 shows the average percentage of schools that were within 5,10 , or 20 percentile ranks in one model versus the other. As can be seen in the table, the PP and MLM0 models ranked schools most similarly, over $50 \%$ of schools were within 10 ranks and over $80 \%$ were within 20 ranks for these two models. The level of agreement in school ranks was much lower when comparing either the PP or the MLM0 models with any of the other models that examined two or more years of achievement. Generally, either the PP or MLM0 model school rankings agreed with the multiyear models within 20 ranks in from about $40 \%$ to $60 \%$ of schools.

Agreement of the multiyear models with each other was greater with from about $50 \%$ to $90 \%$ of models ranking schools within 20 ranks of each other. Some of the lowest agreement in ranks occurred between the average MLM growth rate (AvGrate) rankings and other models, ranging from about $50 \%$ to about $70 \%$ of school within 20 ranks of each other.

Table 12
Proportion of Elementary or Middle Schools within 5, 10, or 20 Ranks of Each Other for each Pair of School Performance Models in Mathematics and Reading/Language Arts Averaged over Cohorts
Model Comparison: $\quad \mathrm{r}=5 \quad \mathrm{r}=10 \quad \mathrm{r}=20$

PP vs. MLM0

| Math Elementary | 0.363 | 0.579 | 0.835 |
| ---: | ---: | ---: | ---: |
| Reading/Language Arts Elementary | 0.370 | 0.584 | 0.840 |
| Math Middle | 0.354 | 0.56 | 0.822 |
| Reading/Language Arts Middle | 0.406 | 0.645 | 0.875 |
| Mean | 0.373 | 0.592 | 0.843 |

## PP vs. Gain

| Math Elementary | 0.147 | 0.251 | 0.441 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.110 | 0.204 | 0.356 |
| Math Middle | 0.178 | 0.306 | 0.501 |
| Reading/Language Arts Middle | 0.097 | 0.180 | 0.326 |
| Mean | 0.133 | 0.235 | 0.406 |

## PP vs. TM

| Math Elementary | 0.160 | 0.276 | 0.471 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.134 | 0.244 | 0.455 |
| Math Middle | 0.217 | 0.357 | 0.583 |
| Reading/Language Arts Middle | 0.178 | 0.298 | 0.498 |
| Mean | 0.172 | 0.294 | 0.502 |

## PP vs. SGP

| Math Elementary | 0.184 | 0.305 | 0.545 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.169 | 0.309 | 0.524 |
| Math Middle | 0.202 | 0.339 | 0.540 |
| Reading/Language Arts Middle | 0.167 | 0.283 | 0.499 |
| Mean | 0.180 | 0.309 | 0.527 |

## PP vs. VAM

|  |  |  |  |
| ---: | ---: | ---: | ---: |
| Math Elementary | 0.183 | 0.32 | 0.554 |
| Reading/Language Arts Elementary | 0.193 | 0.332 | 0.558 |
| Math Middle | 0.193 | 0.325 | 0.534 |
| Reading/Language Arts Middle | 0.150 | 0.270 | 0.495 |
| Mean | 0.180 | 0.312 | 0.535 |

## PP vs. Grate

| Math Elementary | 0.131 | 0.237 | 0.415 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.104 | 0.201 | 0.361 |
| Math Middle | 0.177 | 0.309 | 0.505 |
| Reading/Language Arts Middle | 0.081 | 0.143 | 0.289 |
| Mean | 0.123 | 0.222 | 0.392 |

## PP vs. AvGrate

| Math Elementary | 0.158 | 0.281 | 0.502 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.100 | 0.188 | 0.357 |
| Math Middle | 0.180 | 0.307 | 0.487 |
| Reading/Language Arts Middle | 0.095 | 0.195 | 0.325 |
| Mean | 0.133 | 0.243 | 0.418 |

## MLM0 vs. Gain

| Math Elementary | 0.145 | 0.262 | 0.463 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.098 | 0.185 | 0.348 |
| Math Middle | 0.171 | 0.320 | 0.527 |
| Reading/Language Arts Middle | 0.091 | 0.170 | 0.322 |
| Mean | 0.126 | 0.234 | 0.415 |

## MLM0 vs. TM

| Math Elementary | 0.144 | 0.273 | 0.480 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.132 | 0.237 | 0.421 |
| Math Middle | 0.167 | 0.320 | 0.547 |
| Reading/Language Arts Middle | 0.151 | 0.267 | 0.447 |
| Mean | 0.148 | 0.274 | 0.474 |

## MLM0 vs. SGP

| Math Elementary | 0.189 | 0.345 | 0.576 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.172 | 0.294 | 0.509 |
| Math Middle | 0.189 | 0.339 | 0.554 |
| Reading/Language Arts Middle | 0.166 | 0.270 | 0.508 |
| Mean | 0.179 | 0.312 | 0.537 |

## MLM0 vs. VAM

| Math Elementary | 0.207 | 0.353 | 0.595 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.175 | 0.316 | 0.549 |
| Math Middle | 0.196 | 0.337 | 0.565 |
| Reading/Language Arts Middle | 0.141 | 0.278 | 0.514 |
| Mean | 0.180 | 0.321 | 0.556 |

## MLM0 vs. Grate

| Math Elementary | 0.124 | 0.241 | 0.420 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.088 | 0.181 | 0.337 |
| Math Middle | 0.203 | 0.342 | 0.551 |
| Reading/Language Arts Middle | 0.082 | 0.152 | 0.288 |
| Mean | 0.124 | 0.229 | 0.399 |

## MLM0 vs. AvGrate

| Math Elementary | 0.181 | 0.306 | 0.523 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.099 | 0.183 | 0.349 |
| Math Middle | 0.181 | 0.309 | 0.483 |
| Reading/Language Arts Middle | 0.104 | 0.182 | 0.332 |
| Mean | 0.141 | 0.245 | 0.422 |

## Gain vs. TM

| Math Elementary | 0.404 | 0.631 | 0.875 |
| ---: | :---: | :---: | :---: |
| Reading/Language Arts Elementary | 0.215 | 0.361 | 0.588 |
| Math Middle | 0.421 | 0.636 | 0.866 |
|  | 28 |  |  |


| Reading/Language Arts Middle | 0.232 | 0.416 | 0.624 |
| ---: | :--- | :--- | :--- |
| Mean | 0.318 | 0.511 | 0.738 |

## Gain vs. SGP

| Math Elementary | 0.357 | 0.552 | 0.812 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.206 | 0.341 | 0.552 |
| Math Middle | 0.394 | 0.616 | 0.846 |
| Reading/Language Arts Middle | 0.251 | 0.383 | 0.630 |
| Mean | 0.302 | 0.473 | 0.710 |

## Gain vs. VAM

| Math Elementary | 0.356 | 0.585 | 0.836 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.192 | 0.334 | 0.566 |
| Math Middle | 0.439 | 0.649 | 0.883 |
| Reading/Language Arts Middle | 0.222 | 0.368 | 0.649 |
| Mean | 0.302 | 0.484 | 0.734 |

## Gain vs. Grate

| Math Elementary | 0.583 | 0.823 | 0.98 |
| ---: | :--- | :--- | ---: |
| Reading/Language Arts Elementary | 0.334 | 0.524 | 0.715 |
| Math Middle | 0.553 | 0.816 | 0.971 |
| Reading/Language Arts Middle | 0.468 | 0.739 | 0.938 |
| Mean | 0.485 | 0.726 | 0.901 |

Gain vs. AvGrate

| Math Elementary | 0.211 | 0.371 | 0.597 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.198 | 0.358 | 0.571 |
| Math Middle | 0.265 | 0.399 | 0.626 |
| Reading/Language Arts Middle | 0.237 | 0.373 | 0.617 |
| Mean | 0.228 | 0.375 | 0.603 |

## TM vs. SGP

| Math Elementary | 0.329 | 0.512 | 0.782 |
| ---: | :---: | :---: | :---: |
| Reading/Language Arts Elementary | 0.256 | 0.423 | 0.652 |
|  | 29 |  |  |


| Math Middle | 0.335 | 0.534 | 0.776 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Middle | 0.314 | 0.464 | 0.716 |
| Mean | 0.308 | 0.483 | 0.732 |

## TM vs. VAM

| Math Elementary | 0.327 | 0.520 | 0.783 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.246 | 0.401 | 0.662 |
| Math Middle | 0.333 | 0.538 | 0.791 |
| Reading/Language Arts Middle | 0.270 | 0.443 | 0.727 |
| Mean | 0.294 | 0.476 | 0.741 |

## TM vs. Grate

| Math Elementary | 0.337 | 0.544 | 0.807 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.228 | 0.397 | 0.656 |
| Math Middle | 0.368 | 0.584 | 0.822 |
| Reading/Language Arts Middle | 0.203 | 0.347 | 0.553 |
| Mean | 0.284 | 0.468 | 0.710 |

## TM vs. AvGrate

| Math Elementary | 0.201 | 0.356 | 0.575 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.166 | 0.292 | 0.487 |
| Math Middle | 0.225 | 0.383 | 0.597 |
| Reading/Language Arts Middle | 0.163 | 0.298 | 0.498 |
| Mean | 0.189 | 0.332 | 0.539 |

## SGP vs. VAM

| Math Elementary | 0.575 | 0.822 | 0.974 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.430 | 0.679 | 0.907 |
| Math Middle | 0.598 | 0.833 | 0.974 |
| Reading/Language Arts Middle | 0.425 | 0.700 | 0.920 |
| Mean | 0.507 | 0.758 | 0.944 |

## SGP vs. Grate

| Math Elementary | 0.256 | 0.439 | 0.678 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.188 | 0.329 | 0.552 |
| Math Middle | 0.316 | 0.464 | 0.723 |
| Reading/Language Arts Middle | 0.177 | 0.298 | 0.506 |
| Mean | 0.234 | 0.382 | 0.615 |

## SGP vs. AvGrate

| Math Elementary | 0.317 | 0.526 | 0.770 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.216 | 0.360 | 0.582 |
| Math Middle | 0.337 | 0.556 | 0.807 |
| Reading/Language Arts Middle | 0.222 | 0.369 | 0.615 |
| Mean | 0.273 | 0.453 | 0.694 |

## VAM vs. Grate

| Math Elementary | 0.267 | 0.440 | 0.689 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.210 | 0.355 | 0.573 |
| Math Middle | 0.311 | 0.497 | 0.745 |
| Reading/Language Arts Middle | 0.181 | 0.331 | 0.539 |
| Mean | 0.242 | 0.406 | 0.636 |

## Grate vs. AvGrate

| Math Elementary | 0.169 | 0.288 | 0.501 |
| ---: | :--- | :--- | :--- |
| Reading/Language Arts Elementary | 0.138 | 0.256 | 0.438 |
| Math Middle | 0.204 | 0.329 | 0.517 |
| Reading/Language Arts Middle | 0.191 | 0.337 | 0.551 |
| Mean | 0.176 | 0.302 | 0.502 |

Our last criterion for comparing school ranks across cohorts was the RMSD between pairs of school performance model rankings. Appendix E shows the RMSD between pairs of school performance model rankings for each individual cohort. Table 13 shows the RMSD averaged over the three cohorts by content area and grade level band. The RMSD values reflect the same patterns of results for models as described previously. The greatest agreement in average ranks was between the PP and MLM0 models for which schools differed by about 16 ranks or less on average. Much larger differences (about 30 ranks or more on average) occurred between the PP and MLM0 versus the other school performance models. Agreement in school ranks between the remaining models was generally greater, in the range of 10 to 20 ranks on
average, although differences were somewhat larger between the AvGrate ranks and school ranks based on other models.

Table 13
Average across Cohorts of RMSD in School Ranks between School Performance Models by Content Area and Grade Level Band

Elementary School Mathematics

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 14.868 | 34.971 | 33.024 | 29.202 | 28.273 | 36.925 | 32.098 |
| MLM0 |  | 34.243 | 33.067 | 27.245 | 26.140 | 36.416 | 30.701 |
| Gain |  |  | 13.260 | 15.971 | 14.623 | 7.943 | 26.889 |
| TM |  |  |  | 17.755 | 17.273 | 15.952 | 27.520 |
| SGP |  |  |  |  | 8.322 | 21.691 | 18.523 |
| VAM |  |  |  |  |  | 21.036 | 16.848 |
| Grate |  |  |  |  |  |  | 32.773 |

## Elementary School Reading/Language Arts

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 14.712 | 41.170 | 34.889 | 30.196 | 28.243 | 40.873 | 41.440 |
| MLM0 |  | 42.355 | 36.270 | 30.064 | 28.287 | 42.658 | 42.537 |
| Gain |  |  | 29.216 | 28.802 | 27.719 | 23.478 | 27.504 |
| TM |  |  |  | 22.765 | 22.238 | 23.411 | 31.715 |
| SGP |  |  |  |  | 11.868 | 28.201 | 26.374 |
| VAM |  |  |  |  |  | 27.033 | 25.169 |
| Grate |  |  |  |  |  |  | 34.942 |

Middle School Mathematics

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 16.219 | 30.145 | 26.924 | 28.58 | 28.258 | 30.096 | 32.242 |
| MLM0 |  | 28.676 | 27.745 | 27.155 | 26.782 | 28.209 | 31.953 |
| Gain |  |  | 14.457 | 14.683 | 12.932 | 8.326 | 24.913 |


| TM | 18.225 | 17.644 | 15.777 | 26.607 |
| ---: | ---: | ---: | ---: | ---: |
| SGP |  | 8.330 | 20.216 | 16.257 |
| VAM |  | 19.246 | 14.308 |  |
| Grate |  |  | 30.695 |  |

Middle School Reading/Language Arts

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 13.470 | 43.525 | 33.005 | 31.943 | 31.717 | 46.231 | 43.532 |
| MLM0 |  | 45.499 | 35.079 | 32.500 | 32.284 | 47.907 | 44.730 |
| Gain |  |  | 23.929 | 24.510 | 23.046 | 10.437 | 25.334 |
| TM |  |  |  | 21.508 | 20.289 | 27.575 | 31.313 |
| SGP |  |  |  |  | 11.374 | 30.572 | 25.692 |
| VAM |  |  |  |  |  | 29.257 | 23.367 |
| Grate |  |  |  |  |  |  | 30.083 |

We also evaluated the extent to which school ranks agreed from one content area to the other. Table 14 shows the Spearman's correlation of school ranks in mathematics with school ranks in reading/language arts by cohort and grade level band. The table also shows the mean correlation across cohorts at the two grade level bands. As can be seen in Table 14, on average correlations of school ranks across mathematics and reading/language arts in elementary schools ranged from +.301 to +.839 for the different school performance models. For middle schools, the average correlations ranged from +.160 to +.759 . Correlations were higher for the two status models, and lower for the multiyear models at both grade level bands. Generally, correlations across content were lower for the other models. Average correlations at the middle school level were also consistently lower than for elementary schools for all models.

Table 14
Spearman's Correlations of School Performance Model Estimates across Mathematics and Reading/Language Arts by Cohort

| Elementary Schools |  |  |  |  | Middle Schools |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Model | Cohort 1 | Cohort 2 | Cohort 3 | Mean | Cohort 1 | Cohort 2 | Cohort 3 | Mean |
| PP | 0.781 | 0.755 | 0.755 | 0.764 | 0.716 | 0.693 | 0.659 | 0.689 |
| MLM0 | 0.855 | 0.840 | 0.823 | 0.839 | 0.789 | 0.735 | 0.754 | 0.759 |
| Gain | 0.550 | 0.465 | -0.112 | 0.301 | 0.243 | 0.282 | 0.232 | 0.252 |
| TM | 0.443 | 0.396 | 0.383 | 0.407 | 0.245 | 0.310 | 0.344 | 0.300 |
| SGP | 0.550 | 0.476 | 0.521 | 0.516 | 0.401 | 0.347 | 0.377 | 0.375 |


| VAM | 0.576 | 0.546 | 0.569 | 0.564 | 0.440 | 0.364 | 0.457 | 0.420 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Grate | 0.572 | 0.441 | 0.356 | 0.456 | 0.173 | 0.186 | 0.122 | 0.160 |
| AvGrate | 0.529 | 0.579 | 0.515 | 0.541 | 0.417 | 0.450 | 0.427 | 0.431 |

Table 15 shows the proportion of schools that shared similar ranks in mathematics as in reading/language arts for each school performance model by school level and averaged over grade level band. Similar to results previously described, Table 15 shows greater agreement for the PP and MLM0 models than the other school performance models with about $70 \%$ or more of the schools having ranks within 20 places across grade level bands. In contrast, there was substantially less agreement across the two content areas for the remaining, multiyear models with only approximately $50 \%$ of schools agreeing within 20 ranks for most models in either grade level band.

Table 15
Proportion of Elementary or Middle Schools within 5, 10, or 20 Ranks of Each Other in Mathematics versus Reading/Language Arts for each School Performance Model Averaged over Cohorts

| Model Comparison | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |  |
| :--- | :--- | :--- | :--- | :--- |
| $\underline{\text { PP }}$ |  |  |  |  |
|  |  |  |  |  |
|  | Elementary | 0.316 | 0.500 | 0.741 |
|  | Middle | 0.270 | 0.440 | 0.675 |
|  | Mean | 0.293 | 0.470 | 0.708 |
| $\underline{\text { MLM0 }}$ |  |  |  |  |
| Elementary | 0.339 | 0.547 | 0.805 |  |
| Middle | 0.287 | 0.473 | 0.741 |  |
| Mean | 0.313 | 0.510 | 0.773 |  |

Gain

| Elementary | 0.144 | 0.276 | 0.493 |
| ---: | :--- | :--- | :--- |
| Middle | 0.150 | 0.278 | 0.481 |
| Mean | 0.147 | 0.277 | 0.487 |

TM

| Elementary | 0.161 | 0.295 | 0.521 |
| ---: | :--- | :--- | :--- |
| Middle | 0.143 | 0.284 | 0.499 |
| Mean | 0.152 | 0.290 | 0.510 |

## SGP

| Elementary | 0.198 | 0.340 | 0.556 |
| ---: | :--- | :--- | :--- |
| Middle | 0.166 | 0.274 | 0.490 |
| Mean | 0.182 | 0.307 | 0.523 |

VAM

$$
\begin{array}{rccc}
\text { Elementary } & 0.197 & 0.351 & 0.573 \\
\text { Middle } & 0.162 & 0.292 & 0.495 \\
\text { Mean } & 0.180 & 0.322 & 0.534
\end{array}
$$

## Grate

| Elementary | 0.172 | 0.316 | 0.532 |
| ---: | :--- | :--- | :--- |
| Middle | 0.132 | 0.239 | 0.460 |
| Mean | 0.152 | 0.277 | 0.496 |

AvGrate

| Elementary | 0.190 | 0.339 | 0.564 |
| ---: | :---: | :---: | :---: |
| Middle | 0.176 | 0.291 | 0.538 |
| Mean | 0.183 | 0.315 | 0.551 |

Calculation of the RMSD in school ranks for mathematics versus reading/language arts by cohort and grade level band and averaged over cohorts showed similar results (see Table 16). The difference in school ranks averaged over cohorts for the PP and MLM0 models ranged from about 16 to 22 . Average differences in rank across the two content areas were substantially greater for the remaining models ranging from 20 to 37 depending on model and grade level band.

Table 16
RMSD in School Ranks for Mathematics and Reading/Language Arts by Cohort and Grade Level Band and Overall Means and Standard Deviations (SD)

| Elementary Schools |  |  |  |  | Middle Schools |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Model | Cohort 1 | Cohort 2 | Cohort 3 | Mean | Cohort 1 | Cohort 2 | Cohort 3 | Mean |
| PP | 18.842 | 19.929 | 19.925 | 19.565 | 21.421 | 22.277 | 23.507 | 22.402 |
| MLM0 | 15.348 | 16.091 | 16.953 | 16.131 | 18.494 | 20.713 | 19.947 | 19.718 |
| Gain | 27.018 | 29.447 | 42.488 | 32.984 | 35.015 | 34.106 | 35.280 | 34.800 |
| TM | 30.044 | 31.282 | 31.667 | 30.998 | 34.945 | 33.477 | 32.626 | 33.683 |
| SGP | 27.007 | 29.155 | 27.882 | 28.015 | 31.148 | 32.517 | 31.749 | 31.805 |
| VAM | 26.227 | 27.137 | 26.445 | 26.603 | 30.117 | 32.090 | 29.670 | 30.626 |
| Grate | 26.340 | 30.094 | 32.333 | 29.589 | 36.600 | 36.302 | 37.713 | 36.872 |
| AvGrate | 27.646 | 26.131 | 28.034 | 27.270 | 30.718 | 29.842 | 30.472 | 30.344 |

Relation with school composition variables. We computed the correlation of school ranks based on each school performance model with school composition variables to determine whether estimates were related to the aggregated student characteristics in each school. Table 17 shows these correlations for mathematics and reading/language arts in the elementary school and middle school samples. Correlations of model estimates with school composition variables
within each individual cohort are presented in Appendix F. The rightmost column of Table 17 shows the correlation of each school performance model averaged over all of the school composition variables. As can be seen, correlations of the status models, PP and MLM0, ranged from -. 153 to -.284 depending on content and grade level band and were noticeably higher than the correlations of the other school performance models with school composition variables, which ranged from -.010 to +.181 depending on content and grade level band.

Table 17
Spearman's Correlations of School Ranks with School Composition Variables by Content Area and Grade Level Band

Elementary School Mathematics

|  |  |  |  | Ethnic |  |  | School |  |
| ---: | ---: | ---: | ---: | ---: | ---: | :--- | ---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |  |
| PP | -0.526 | -0.323 | -0.205 | 0.001 | -0.282 | 0.123 | -0.202 |  |
| MLM0 | -0.616 | -0.301 | -0.184 | -0.009 | -0.272 | 0.213 | -0.195 |  |
| Gain | -0.015 | 0.053 | 0.008 | -0.003 | 0.022 | 0.114 | 0.030 |  |
| TM | -0.053 | 0.020 | -0.011 | -0.011 | -0.012 | 0.102 | 0.006 |  |
| SGP | -0.159 | -0.013 | -0.039 | -0.005 | -0.014 | 0.172 | -0.010 |  |
| VAM | -0.183 | -0.017 | -0.053 | 0.013 | -0.025 | 0.188 | -0.013 |  |
| Grate | -0.006 | 0.034 | 0.025 | -0.011 | -0.002 | 0.071 | 0.018 |  |
| AvGrate | -0.029 | 0.086 | -0.027 | 0.038 | 0.081 | 0.173 | 0.054 |  |

Elementary School Reading/Language Arts

|  |  |  |  |  | Ethnic | School |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.610 | -0.491 | -0.201 | 0.002 | -0.426 | 0.040 | -0.281 |
| MLM0 | -0.722 | -0.480 | -0.181 | -0.004 | -0.437 | 0.123 | -0.284 |
| Gain | 0.153 | 0.174 | 0.083 | -0.027 | 0.134 | 0.060 | 0.096 |
| TM | -0.085 | 0.031 | 0.039 | -0.026 | 0.018 | 0.089 | 0.011 |
| SGP | -0.225 | -0.062 | -0.043 | 0.001 | -0.083 | 0.112 | -0.050 |
| VAM | -0.264 | -0.095 | -0.049 | 0.006 | -0.110 | 0.126 | -0.064 |
| Grate | 0.139 | 0.116 | 0.058 | 0.000 | 0.089 | 0.007 | 0.068 |
| AvGrate | 0.224 | 0.273 | 0.060 | 0.005 | 0.202 | 0.054 | 0.136 |

Middle School Mathematics

|  |  |  |  |  | Ethnic | School |  |
| ---: | :---: | ---: | ---: | ---: | ---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.385 | -0.211 | -0.266 | 0.040 | -0.213 | 0.119 | -0.153 |


| MLM0 | -0.488 | -0.149 | -0.178 | 0.005 | -0.141 | 0.203 | -0.125 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Gain | -0.034 | 0.045 | -0.013 | -0.013 | 0.058 | 0.147 | 0.032 |
| TM | -0.094 | 0.008 | -0.070 | -0.010 | 0.004 | 0.158 | -0.001 |
| SGP | -0.015 | 0.085 | -0.016 | 0.000 | 0.081 | 0.173 | 0.051 |
| VAM | -0.011 | 0.074 | -0.023 | 0.002 | 0.074 | 0.168 | 0.047 |
| Grate | -0.112 | -0.008 | -0.037 | -0.020 | 0.017 | 0.134 | -0.004 |
| AvGrate | 0.119 | 0.134 | 0.002 | 0.019 | 0.112 | 0.130 | 0.086 |

Middle School Reading/Language Arts

|  |  |  |  |  | Ethnic | School |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.559 | -0.385 | -0.272 | 0.133 | -0.401 | 0.053 | -0.239 |
| MLM0 | -0.687 | -0.369 | -0.241 | 0.108 | -0.394 | 0.105 | -0.246 |
| Gain | 0.338 | 0.227 | 0.136 | -0.021 | 0.192 | 0.030 | 0.150 |
| TM | -0.031 | 0.029 | 0.017 | 0.043 | -0.002 | 0.137 | 0.032 |
| SGP | -0.075 | 0.027 | -0.021 | 0.051 | -0.019 | 0.119 | 0.014 |
| VAM | -0.055 | 0.034 | -0.019 | 0.039 | -0.030 | 0.103 | 0.012 |
| Grate | 0.381 | 0.238 | 0.165 | -0.055 | 0.207 | 0.009 | 0.158 |
| AvGrate | 0.398 | 0.311 | 0.132 | -0.022 | 0.227 | 0.038 | 0.181 |

Relation of school ranks with SWD school composition. We also specifically examined the relations between the percentage of SWD students served by a school and the school ranks based on the school performance model. Table 18 shows these correlations for mathematics and reading/language arts in the elementary school and middle school samples averaged over cohorts. Correlations of model estimates with SWD school composition within each individual cohort are presented in Appendix G. As can be seen in the bottom row of Table 18 , on average, there was a substantially higher correlation of the status models (PP and MLM0) with school SWD composition than the other school performance models. With the PP and MLM0 models, school ranks were higher with lower percentages of SWD students in the school and school ranks were lower as schools served larger proportions of SWD. Little relation was present between school ranks based on the other models and SWD school composition.

Table 18
Average School Rank as a Function of the Percentage of SWD in the School by Model, Content Area, and Grade Level Band

| Content Area and |  |  |  |  |  |  |  |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | ---: |
| Grade Level Band | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| Math Elementary | -0.205 | -0.184 | 0.008 | -0.011 | -0.039 | -0.053 | 0.025 | -0.027 |
| Reading/Language | -0.201 | -0.181 | 0.083 | 0.039 | -0.043 | -0.049 | 0.058 | 0.060 |
| Arts Elementary |  |  |  |  |  |  |  |  |


| Math Middle | -0.266 | -0.178 | -0.013 | -0.070 | -0.016 | -0.023 | -0.037 | 0.002 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Reading/Language | -0.272 | -0.241 | 0.136 | 0.017 | -0.021 | -0.019 | 0.165 | 0.132 |
| Arts Middle |  |  |  |  |  |  |  |  |
| Mean | -0.236 | -0.196 | 0.054 | -0.006 | -0.030 | -0.036 | 0.053 | 0.042 |

Summary of Section B. We evaluated the school ranks arising from eight alternative models for estimating school academic performance in mathematics and reading/language arts across three sequential cohorts of students. As with the school performance estimates described in Section A, substantial variability in school ranks was present across the three student cohorts regardless of content area or grade level band. Using any of our comparison criteria (Spearman's correlations, absolute difference in ranks, RMSD), there was somewhat less variability across cohorts for status models (PP and MLM0) than for the models that used more than one year of data. When we compared school ranks arising from one model to school ranks from other models, we found substantial disagreement across models. Generally, the PP and MLM0 status models were more similar to each other and both differed from the remaining models that examined more than one year of data. Comparison of model estimates to school composition variables showed that the status models (PP and MLM0) had substantially higher correlations than the remaining school performance models. Finally, we correlated school ranks arising from the eight performance models with the percentage of SWD in each school. As with the school performance model estimates, we found that the status models were more highly correlated with SWD school composition but there was little relation of the other model estimates with the percentage of SWD students in the school.

## Conclusion

This technical report described the Oregon results of a large study examining eight alternative methods of estimating school performance. We represented school performance in two ways, the actual model estimates and school ranks based on model estimates. In addition to this Oregon report, there are additional reports describing results for the three other states (AZ, NC, PA) included in the study that are available at www.ncaase.com.

A number of general conclusions can be drawn from the results of the Oregon analyses. First, model representations of school performance over successive cohorts of students were very unstable, irrespective of whether representations were based on school performance model estimates or on school ranks. There was somewhat greater stability over cohorts for status models (PP, MLM0) than for the multiyear models. Nonetheless, even with the most stable model, MLM0, Spearman's correlations showed that less than two-thirds of the variance was common across cohorts, and over all the models, there was substantial instability over cohorts. These results were also reflected in the examination of differences in absolute or average (RMSD) differences in ranks over cohorts.

Our examination of the relations of the school performance models with each other produced similar results. Generally, there was agreement between the two status model estimates (PP and MLM0) that were based on a single year of data, but these two models did not agree with the remaining multiyear models. However, there was some substantial agreement of the multiyear models with each other with some variations. In general, the AvGrate model showed the least agreement with the other multiyear models.

We also examined the relation of school performance model estimates with variables describing the student composition of the schools. These results showed a pattern of results that differed between the status and the multiyear models. The two status models had substantially higher correlations with school composition variables than the multiyear models. This was also true in terms of the percentage of SWD students served by a school. The higher the percentage of SWD in the school, the lower the status model estimates of school performance.

Thus, the Oregon results showed consistent patterns of instability of estimates of school performance over successive cohorts of students, different estimates of school performance depending on the model chosen, especially for status versus multiyear models, and stronger relations of status models with the student composition of the school than multiyear models. Taken together, these results suggest the need for substantial caution in the way that school performance models are used and interpreted. Cohort instability suggests that rolling averages or some other mechanism is needed to provide more dependable depictions of school performance that are more stable over time. The substantial disagreement among the school performance models suggests that the choice of model matters a great deal. This choice should be made very carefully. A single model estimate of school performance may not be trustworthy and may need to be augmented by the results from additional models or metrics of school performance.

## References

Ballou, D., Sanders, W., \& Wright, P. (2004). Controlling for student background in value-added assessment of teachers. Journal of Educational and Behavioral Statistics, 29(1), 37-65.

Betebenner, D. (2009). Norm-and criterion-referenced student growth. Educational Measurement: Issues and Practice, 28(4), 42-51.

Betebenner, D. W., \& Iwaarden, A. V. (2011). SGP: An textupR package for the calculation and visualization of student growth percentiles [Computer software manual]. (R package version 0.4-0.0 available at http://cran.r-project.org/web/packages/SGP/)

Bloom, H. S., Hill, C. J., Black, A. R., \& Lipsey, M. W. (2008). Performance trajectories and performance gaps as achievement effect-size benchmarks for educational interventions. Journal of Research on Educational Effectiveness, 1, 289-328.

Castellano, K. E., \& Ho, A. D. (2013). Contrasting OLS and Quantile Regression Approaches to Student "Growth" Percentiles. Journal of Educational and Behavioral Statistics, 38, 190215.

Goldschmidt, P., Choi, K., \& Beaudoin, J. P. (2012, February). Growth model comparison study: Practical implications of alternative models for evaluating school performance. Council of Chief State School Officers: Washington, DC.

Oregon Department of Education (ODE). (2008). Technical report: Oregon's statewide assessment system test development. Standard Setting, Volume 3. Salem, OR.

Oregon Department of Education. (2009, January). 2007-2008 technical report: Score interpretation guide. Retrieved from ODE website:
http://www.ode.state.or.us/teachlearn/testing/manuals/2008/asmttechmanualvol6_interpgui de.pdf

Oregon Department of Education (ODE). (2012a). Technical report: Oregon's statewide assessment system test development, Volumes 1-10. Salem, OR.

Oregon Department of Education (ODE). (2012b). Technical report: Oregon's statewide assessment system test development. Test Administration, Volume 5. Salem, OR.

Raudenbush, S. W., \& Bryk, A. S. (2002). Hierarchical linear models: Applications and data analysis methods ( $2^{\text {nd }}$ ed.). Thousand Oaks, CA: Sage Publications, Inc.

Raudenbush, S. W., Bryk, A. S., Cheong, Y. F., Congdon, R. T., \& du Toit, M. (2011). HLM 7: Hierarchical linear and nonlinear modeling. Lincolnwood, IL: Scientific Software International.

Tindal, G., Nese, J. F. T., and Stevens, J. J. (2017). Estimating school effects with a state testing program using transition matrices. Educational Assessment, 22, 189-204.

## Appendix A

Correlations among School Performance Model Estimates for Each Individual Cohort by Content Area and Grade Level Band.

Mathematics Elementary Schools
Cohort 1

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.805 | 0.150 | 0.295 | 0.465 | 0.473 | 0.049 | 0.254 |  |
| MLM0 |  | 0.129 | 0.236 | 0.521 | 0.567 | 0.003 | 0.336 |  |
| Gain |  |  | 0.887 | 0.816 | 0.832 | 0.952 | 0.515 |  |
| TM |  |  |  | 0.792 | 0.796 | 0.827 | 0.496 |  |
| SGP |  |  |  |  | 0.956 | 0.659 | 0.756 |  |
| VAM |  |  |  |  |  | 0.665 | 0.800 |  |
| Grate |  |  |  |  |  |  | 0.253 |  |

Cohort 2

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.832 | 0.364 | 0.375 | 0.527 | 0.542 | 0.296 | 0.426 |  |
| MLM0 |  | 0.372 | 0.313 | 0.546 | 0.584 | 0.321 | 0.421 |  |
| Gain |  |  | 0.901 | 0.892 | 0.916 | 0.970 | 0.691 |  |
| TM |  |  |  | 0.826 | 0.826 | 0.865 | 0.640 |  |
| SGP |  |  |  |  | 0.961 | 0.800 | 0.851 |  |
| VAM |  |  |  |  |  | 0.822 | 0.890 |  |
| Grate |  |  |  |  |  |  | 0.520 |  |

Cohort 3

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.842 | 0.268 | 0.405 | 0.494 | 0.534 | 0.161 | 0.469 |  |
| MLM0 |  | 0.328 | 0.400 | 0.583 | 0.625 | 0.214 | 0.520 |  |
| Gain |  |  |  |  |  |  |  |  |
|  |  |  | 0.893 | 0.83 | 0.868 | 0.959 | 0.512 |  |


| TM | 0.817 | 0.820 | 0.838 | 0.511 |
| ---: | :--- | :--- | :--- | :--- |
| SGP |  | 0.955 | 0.692 | 0.803 |
| VAM |  |  | 0.719 | 0.840 |
| Grate |  |  |  | 0.267 |

AvGrate

Mathematics Middle Schools
Cohort 1

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.770 | 0.360 | 0.530 | 0.435 | 0.421 | 0.306 | 0.287 |  |
| MLM0 |  | 0.383 | 0.389 | 0.460 | 0.520 | 0.342 | 0.372 |  |
| Gain |  |  | 0.845 | 0.839 | 0.878 | 0.932 | 0.500 |  |
| TM |  |  |  | 0.719 | 0.705 | 0.781 | 0.366 |  |
| SGP |  |  |  |  | 0.931 | 0.671 | 0.780 |  |
| VAM |  |  |  |  |  | 0.723 | 0.833 |  |
| Grate |  |  |  |  |  |  | 0.229 |  |

Cohort 2

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.796 | 0.425 | 0.523 | 0.535 | 0.512 | 0.393 | 0.354 |  |
| MLM0 |  | 0.378 | 0.409 | 0.481 | 0.500 | 0.388 | 0.287 |  |
| Gain |  |  | 0.889 | 0.897 | 0.913 | 0.957 | 0.669 |  |
| TM |  |  |  | 0.844 | 0.844 | 0.840 | 0.640 |  |
| SGP |  |  |  |  | 0.953 | 0.783 | 0.841 |  |
| VAM |  |  |  |  |  | 0.818 | 0.886 |  |
| Grate |  |  |  |  |  |  | 0.484 |  |

Cohort 3

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.790 | 0.583 | 0.662 | 0.568 | 0.591 | 0.594 | 0.502 |  |


| MLM0 | 0.638 | 0.616 | 0.596 | 0.620 | 0.706 | 0.457 |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- |
| Gain |  | 0.927 | 0.904 | 0.936 | 0.965 | 0.759 |
| TM |  |  | 0.870 | 0.877 | 0.887 | 0.726 |
| SGP |  |  |  | 0.962 | 0.832 | 0.901 |
| VAM |  |  |  |  | 0.868 | 0.932 |
| Grate |  |  |  |  | 0.630 |  |

Reading/Language Arts Elementary Schools
Cohort 1

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.828 | -0.012 | 0.276 | 0.466 | 0.547 | -0.152 | -0.099 |  |
| MLM0 |  | -0.184 | 0.208 | 0.455 | 0.522 | -0.302 | -0.232 |  |
| Gain |  |  | 0.718 | 0.651 | 0.670 | 0.907 | 0.504 |  |
| TM |  |  |  | 0.722 | 0.721 | 0.593 | 0.345 |  |
| SGP |  |  |  |  | 0.917 | 0.409 | 0.501 |  |
| VAM |  |  |  |  |  | 0.435 | 0.529 |  |
| Grate |  |  |  |  |  |  | 0.213 |  |

Cohort 2

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.838 | 0.071 | 0.200 | 0.432 | 0.497 | -0.008 | 0.023 |  |
| MLM0 |  | -0.028 | 0.124 | 0.441 | 0.509 | -0.102 | -0.037 |  |
| Gain |  |  | 0.769 | 0.727 | 0.766 | 0.931 | 0.534 |  |
| TM |  |  |  | 0.673 | 0.684 | 0.685 | 0.456 |  |
| SGP |  |  |  |  | 0.914 | 0.571 | 0.642 |  |
| VAM |  |  |  |  |  | 0.605 | 0.696 |  |
| Grate |  |  |  |  |  |  | 0.286 |  |


| Cohort 3 |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate |
| AvGrate |  |  |  |  |  |  |  |
| PP | 0.865 | -0.104 | 0.303 | 0.445 | 0.512 | 0.122 | -0.055 |
| MLM0 |  | -0.108 | 0.254 | 0.438 | 0.502 | 0.044 | -0.139 |
| Gain |  |  | -0.219 | 0.065 | 0.060 | -0.512 | 0.626 |
| TM |  |  |  | 0.732 | 0.743 | 0.738 | 0.418 |
| SGP |  |  |  |  | 0.909 | 0.624 | 0.618 |
| VAM |  |  |  |  |  | 0.689 | 0.662 |
| Grate |  |  |  |  |  |  | 0.322 |

Reading/Language Arts Middle Schools
Cohort 1

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.851 | -0.197 | 0.383 | 0.390 | 0.347 | -0.357 | -0.192 |  |
| MLM0 |  | -0.352 | 0.227 | 0.324 | 0.291 | -0.501 | -0.321 |  |
| Gain |  |  | 0.624 | 0.646 | 0.690 | 0.916 | 0.616 |  |
| TM |  |  |  | 0.730 | 0.715 | 0.470 | 0.351 |  |
| SGP |  |  |  |  | 0.897 | 0.417 | 0.567 |  |
| VAM |  |  |  |  |  | 0.509 | 0.685 |  |
| Grate |  |  |  |  |  |  | 0.468 |  |

Cohort 2

| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| PP | 0.827 | -0.106 | 0.342 | 0.401 | 0.392 | -0.303 | -0.248 |  |
| MLM0 |  | -0.329 | 0.146 | 0.291 | 0.349 | -0.462 | -0.381 |  |
| Gain |  |  | 0.706 | 0.647 | 0.649 | 0.891 | 0.549 |  |
| TM |  |  |  | 0.683 | 0.657 | 0.517 | 0.277 |  |
| SGP |  |  |  |  | 0.880 | 0.368 | 0.542 |  |


| VAM |  |  |  |  |  | 0.439 | 0.584 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Grate |  |  |  |  |  |  | 0.354 |
| Cohort 3 |  |  |  |  |  |  |  |
| Model | PP | MLM0 | Gain | TM | SGP | VAM | Grate |
| PP AvGrate |  |  |  |  |  |  |  |
| MLM0 | 0.880 | -0.113 | 0.357 | 0.393 | 0.457 | -0.262 | 0.010 |
| Gain |  | -0.208 | 0.306 | 0.412 | 0.462 | -0.351 | -0.048 |
| TM |  |  | 0.705 | 0.689 | 0.686 | 0.942 | 0.642 |
| SGP |  |  |  | 0.783 | 0.786 | 0.592 | 0.524 |
| VAM |  |  |  |  | 0.913 | 0.528 | 0.685 |
| Grate |  |  |  |  |  | 0.549 | 0.776 |

## Appendix B

## Correlations of School Performance Model Estimates with School Composition Variables for each Individual Cohort by Content Area and Grade Level Band.

Mathematics Elementary Schools
Cohort 1

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.457 | -0.333 | -0.201 | -0.017 | -0.315 | 0.148 |
| MLM0 | -0.603 | -0.348 | -0.194 | -0.058 | -0.315 | 0.242 |
| Gain | 0.102 | 0.156 | 0.081 | -0.022 | 0.099 | 0.164 |
| TM | 0.000 | 0.113 | 0.006 | -0.015 | 0.043 | 0.174 |
| SGP | -0.132 | 0.028 | -0.033 | -0.062 | 0.005 | 0.248 |
| VAM | -0.156 | 0.020 | -0.029 | -0.033 | -0.001 | 0.270 |
| Grate | 0.117 | 0.151 | 0.099 | -0.009 | 0.076 | 0.110 |
| AvGrate | 0.025 | 0.141 | -0.014 | -0.010 | 0.149 | 0.223 |

## Cohort 2

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.507 | -0.319 | -0.209 | 0.075 | -0.291 | 0.181 |
| MLM0 | -0.636 | -0.344 | -0.223 | 0.025 | -0.293 | 0.238 |
| Gain | -0.039 | 0.080 | 0.019 | 0.023 | 0.027 | 0.093 |
| TM | -0.001 | 0.108 | -0.012 | 0.046 | 0.042 | 0.093 |
| SGP | -0.122 | 0.026 | -0.014 | 0.031 | -0.001 | 0.142 |
| VAM | -0.146 | 0.029 | -0.041 | 0.045 | 0.000 | 0.170 |
| Grate | -0.052 | 0.051 | 0.019 | 0.017 | -0.005 | 0.063 |
| AvGrate | 0.006 | 0.128 | -0.011 | 0.058 | 0.106 | 0.166 |

## Cohort 3

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | :---: | ---: | :---: |
| PP | -0.536 | -0.334 | -0.172 | -0.021 | -0.351 | 0.111 |
| MLM0 | -0.638 | -0.327 | -0.167 | -0.004 | -0.288 | 0.203 |
| Gain | -0.109 | -0.080 | -0.049 | -0.009 | -0.064 | 0.039 |
| TM | -0.173 | -0.126 | -0.041 | -0.049 | -0.119 | 0.025 |
| SGP | -0.219 | -0.102 | -0.060 | 0.003 | -0.088 | 0.122 |
| VAM | -0.239 | -0.120 | -0.086 | 0.005 | -0.104 | 0.120 |
| Grate | -0.104 | -0.105 | -0.031 | -0.028 | -0.080 | 0.013 |


| AvGrate | -0.092 | 0.000 | -0.058 | 0.033 | -0.007 | 0.121 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mathematics Middle Schools |  |  |  |  |  |  |
| Cohort 1 |  |  |  |  |  |  |
| Model | EDS | EL | SWD | Female | Minority | School Size |
| PP | -0.362 | -0.198 | -0.248 | -0.013 | -0.309 | 0.166 |
| MLM0 | -0.461 | -0.189 | -0.169 | -0.078 | -0.204 | 0.212 |
| Gain | -0.050 | 0.116 | -0.016 | -0.021 | 0.112 | 0.156 |
| TM | -0.076 | 0.117 | -0.132 | 0.011 | 0.024 | 0.227 |
| SGP | -0.005 | 0.130 | 0.039 | -0.009 | 0.103 | 0.165 |
| VAM | -0.031 | 0.118 | 0.024 | -0.038 | 0.089 | 0.188 |
| Grate | -0.109 | 0.055 | -0.038 | -0.054 | 0.068 | 0.135 |
| AvGrate | 0.101 | 0.154 | 0.089 | -0.006 | 0.094 | 0.144 |

## Cohort 2

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.331 | -0.234 | -0.275 | 0.084 | -0.313 | 0.137 |
| MLM0 | -0.472 | -0.258 | -0.180 | 0.096 | -0.210 | 0.221 |
| Gain | 0.039 | -0.018 | -0.058 | 0.032 | -0.040 | 0.065 |
| TM | -0.015 | -0.055 | -0.099 | 0.035 | -0.084 | 0.090 |
| SGP | 0.011 | 0.008 | -0.084 | 0.015 | -0.046 | 0.128 |
| VAM | 0.024 | 0.023 | -0.050 | 0.026 | -0.006 | 0.143 |
| Grate | -0.025 | -0.082 | -0.059 | 0.029 | -0.081 | 0.049 |
| AvGrate | 0.166 | 0.157 | 0.009 | -0.003 | 0.096 | 0.142 |

## Cohort 3

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.296 | -0.254 | -0.278 | 0.082 | -0.175 | 0.205 |
| MLM0 | -0.464 | -0.249 | -0.187 | 0.010 | -0.137 | 0.275 |
| Gain | -0.016 | -0.047 | -0.137 | 0.080 | 0.097 | 0.198 |
| TM | -0.049 | -0.064 | -0.124 | 0.065 | 0.076 | 0.181 |
| SGP | 0.008 | -0.003 | -0.102 | 0.073 | 0.121 | 0.223 |
| VAM | 0.024 | -0.005 | -0.118 | 0.073 | 0.104 | 0.211 |
| Grate | -0.137 | -0.107 | -0.126 | 0.057 | 0.009 | 0.229 |
| AvGrate | 0.133 | 0.072 | -0.096 | 0.070 | 0.151 | 0.165 |

## Reading/Language Arts Elementary Schools

Cohort 1

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.539 | -0.530 | -0.174 | -0.035 | -0.488 | 0.073 |
| MLM0 | -0.671 | -0.511 | -0.187 | -0.025 | -0.464 | 0.153 |
| Gain | 0.212 | 0.201 | 0.130 | 0.001 | 0.122 | 0.086 |
| TM | -0.080 | 0.049 | 0.081 | -0.033 | -0.012 | 0.156 |
| SGP | -0.187 | -0.055 | -0.021 | 0.001 | -0.111 | 0.174 |
| VAM | -0.265 | -0.124 | -0.034 | -0.007 | -0.176 | 0.187 |
| Grate | 0.251 | 0.198 | 0.136 | 0.023 | 0.123 | 0.061 |
| AvGrate | 0.253 | 0.320 | 0.065 | 0.006 | 0.232 | 0.044 |

## Cohort 2

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.610 | -0.506 | -0.255 | 0.013 | -0.472 | 0.078 |
| MLM0 | -0.747 | -0.530 | -0.240 | 0.013 | -0.475 | 0.145 |
| Gain | 0.100 | 0.175 | 0.019 | -0.002 | 0.110 | 0.054 |
| TM | -0.045 | 0.101 | 0.025 | -0.005 | 0.046 | 0.084 |
| SGP | -0.227 | -0.051 | -0.083 | -0.008 | -0.097 | 0.127 |
| VAM | -0.271 | -0.077 | -0.106 | 0.005 | -0.116 | 0.151 |
| Grate | 0.119 | 0.152 | 0.035 | 0.000 | 0.101 | 0.004 |
| AvGrate | 0.184 | 0.272 | 0.026 | -0.002 | 0.190 | 0.105 |

## Cohort 3

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.651 | -0.542 | -0.184 | 0.029 | -0.516 | 0.040 |
| MLM0 | -0.757 | -0.537 | -0.139 | 0.015 | -0.492 | 0.099 |
| Gain | 0.163 | 0.175 | 0.079 | -0.071 | 0.120 | 0.060 |
| TM | -0.091 | 0.004 | 0.000 | 0.046 | -0.010 | 0.011 |
| SGP | -0.215 | -0.078 | -0.019 | -0.002 | -0.108 | 0.029 |
| VAM | -0.239 | -0.129 | -0.037 | 0.027 | -0.130 | 0.038 |
| Grate | 0.057 | 0.041 | -0.009 | 0.046 | 0.047 | -0.050 |
| AvGrate | 0.275 | 0.264 | 0.080 | -0.010 | 0.209 | 0.008 |

## Reading/Language Arts Middle Schools

## Cohort 1

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.505 | -0.412 | -0.342 | 0.197 | -0.496 | 0.104 |
| MLM0 | -0.628 | -0.440 | -0.253 | 0.109 | -0.452 | 0.113 |
| Gain | 0.312 | 0.259 | 0.127 | -0.006 | 0.197 | 0.017 |
| TM | -0.005 | 0.031 | -0.032 | 0.086 | -0.082 | 0.103 |
| SGP | -0.054 | 0.054 | -0.041 | 0.065 | -0.097 | 0.129 |
| VAM | -0.017 | 0.055 | -0.042 | 0.013 | -0.058 | 0.138 |
| Grate | 0.369 | 0.290 | 0.163 | -0.061 | 0.236 | -0.005 |
| AvGrate | 0.412 | 0.360 | 0.102 | -0.067 | 0.249 | 0.074 |

## Cohort 2

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.501 | -0.451 | -0.197 | 0.135 | -0.510 | 0.031 |
| MLM0 | -0.668 | -0.498 | -0.192 | 0.162 | -0.483 | 0.079 |
| Gain | 0.359 | 0.280 | 0.083 | -0.053 | 0.187 | -0.023 |
| TM | 0.032 | 0.050 | 0.063 | 0.014 | -0.032 | 0.042 |
| SGP | -0.007 | 0.033 | 0.033 | 0.008 | -0.036 | 0.093 |
| VAM | -0.033 | -0.002 | -0.023 | 0.055 | -0.087 | 0.064 |
| Grate | 0.369 | 0.257 | 0.102 | -0.057 | 0.178 | -0.058 |
| AvGrate | 0.483 | 0.403 | 0.133 | -0.082 | 0.331 | 0.039 |

## Cohort 3

| Model | EDS | EL | SWD | Female | Minority | School Size |
| ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| PP | -0.569 | -0.468 | -0.251 | 0.072 | -0.438 | 0.129 |
| MLM0 | -0.693 | -0.439 | -0.205 | 0.087 | -0.433 | 0.134 |
| Gain | 0.306 | 0.175 | 0.065 | -0.018 | 0.294 | 0.099 |
| TM | -0.090 | -0.078 | -0.033 | 0.007 | 0.031 | 0.191 |
| SGP | -0.128 | -0.038 | -0.097 | 0.096 | -0.009 | 0.163 |
| VAM | -0.124 | -0.048 | -0.048 | 0.053 | -0.028 | 0.162 |
| Grate | 0.357 | 0.219 | 0.113 | -0.044 | 0.292 | 0.085 |
| AvGrate | 0.287 | 0.254 | 0.060 | 0.033 | 0.195 | 0.058 |

## Appendix C

## Correlations of School Performance Model Estimates with School Percentage SWD for each Individual Cohort by Content Area and Grade Level Band.

Mathematics Elementary Schools

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | -0.201 | -0.194 | 0.081 | 0.006 | -0.033 | -0.029 | 0.099 | -0.014 |
| 2 | -0.209 | -0.223 | 0.019 | -0.012 | -0.014 | -0.041 | 0.019 | -0.011 |
| 3 | -0.172 | -0.167 | -0.049 | -0.041 | -0.060 | -0.086 | -0.031 | -0.058 |

Mathematics Middle Schools

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | -0.248 | -0.169 | -0.016 | -0.132 | 0.039 | 0.024 | -0.038 | 0.089 |
| 2 | -0.275 | -0.180 | -0.058 | -0.099 | -0.084 | -0.050 | -0.059 | 0.009 |
| 3 | -0.278 | -0.187 | -0.137 | -0.124 | -0.102 | -0.118 | -0.126 | -0.096 |

Reading/Language Arts Elementary Schools

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | -0.174 | -0.187 | 0.130 | 0.081 | -0.021 | -0.034 | 0.136 | 0.065 |
| 2 | -0.255 | -0.240 | 0.019 | 0.025 | -0.083 | -0.106 | 0.035 | 0.026 |
| 3 | -0.184 | -0.139 | 0.079 | 0.000 | -0.019 | -0.037 | -0.009 | 0.080 |

Reading/Language Arts Middle Schools

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | -0.342 | -0.253 | 0.127 | -0.032 | -0.041 | -0.042 | 0.163 | 0.102 |
| 2 | -0.197 | -0.192 | 0.083 | 0.063 | 0.033 | -0.023 | 0.102 | 0.133 |
| 3 | -0.251 | -0.205 | 0.065 | -0.033 | -0.097 | -0.048 | 0.113 | 0.060 |

## Appendix D

Proportion of Elementary or Middle Schools within 5, 10, or 20 Ranks of Each Other for each Pair of School Performance Models in Mathematics and Reading/Language Arts by Cohort.

|  | Cohort 1 |  |  | Cohort 2 |  |  | Cohort 3 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Comparison | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ | $r=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ | $\mathrm{r}=5$ | $\mathrm{r}=10$ | $\mathrm{r}=20$ |
| $\underline{\text { PP vs. MLM0 }}$ |  |  |  |  |  |  |  |  |  |
| Math Elementary | 0.315 | 0.536 | 0.835 | 0.401 | 0.594 | 0.838 | 0.373 | 0.606 | 0.832 |
| Reading/Language Arts Elementary | 0.366 | 0.563 | 0.823 | 0.341 | 0.581 | 0.834 | 0.404 | 0.609 | 0.863 |
| Math Middle | 0.370 | 0.560 | 0.819 | 0.342 | 0.605 | 0.844 | 0.350 | 0.514 | 0.802 |
| Reading/Language Arts Middle | 0.428 | 0.663 | 0.881 | 0.387 | 0.617 | 0.848 | 0.403 | 0.654 | 0.897 |
| Mean | 0.370 | 0.580 | 0.839 | 0.368 | 0.599 | 0.841 | 0.382 | 0.596 | 0.848 |

## PP vs. Gain

| Math Elementary | 0.149 | 0.236 | 0.421 | 0.150 | 0.276 | 0.472 | 0.144 | 0.243 | 0.431 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.109 | 0.199 | 0.359 | 0.121 | 0.209 | 0.371 | 0.101 | 0.204 | 0.338 |
| Math Middle | 0.119 | 0.243 | 0.428 | 0.206 | 0.333 | 0.490 | 0.210 | 0.342 | 0.584 |
| Reading/Language <br> Arts Middle | 0.107 | 0.177 | 0.342 | 0.099 | 0.181 | 0.317 | 0.086 | 0.181 | 0.321 |
| Mean | 0.121 | 0.214 | 0.388 | 0.144 | 0.250 | 0.412 | 0.135 | 0.242 | 0.418 |

## $\underline{\text { PP vs. TM }}$

| Math Elementary | 0.160 | 0.257 | 0.469 | 0.165 | 0.285 | 0.470 | 0.155 | 0.284 | 0.474 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.132 | 0.257 | 0.469 | 0.129 | 0.215 | 0.427 | 0.139 | 0.260 | 0.470 |


| Math Middle | 0.169 | 0.317 | 0.551 | 0.210 | 0.379 | 0.580 | 0.272 | 0.374 | 0.617 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.144 | 0.300 | 0.481 | 0.181 | 0.276 | 0.490 | 0.210 | 0.317 | 0.523 |
| Arts Middle |  |  |  |  |  |  |  |  |  |
| Mean | 0.151 | 0.283 | 0.492 | 0.171 | 0.289 | 0.492 | 0.194 | 0.309 | 0.521 |

## PP vs. SGP

| Math Elementary | 0.178 | 0.305 | 0.525 | 0.205 | 0.309 | 0.548 | 0.168 | 0.302 | 0.561 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.180 | 0.315 | 0.538 | 0.137 | 0.275 | 0.492 | 0.189 | 0.338 | 0.543 |
| Math Middle | 0.177 | 0.296 | 0.502 | 0.214 | 0.362 | 0.551 | 0.214 | 0.358 | 0.568 |
| Reading/Language <br> Arts Middle | 0.202 | 0.292 | 0.506 | 0.140 | 0.280 | 0.465 | 0.160 | 0.276 | 0.527 |
| Mean | 0.184 | 0.302 | 0.518 | 0.174 | 0.306 | 0.514 | 0.183 | 0.318 | 0.550 |

## PP vs. VAM

| Math Elementary | 0.186 | 0.318 | 0.540 | 0.186 | 0.318 | 0.554 | 0.175 | 0.323 | 0.569 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.194 | 0.344 | 0.588 | 0.171 | 0.291 | 0.520 | 0.215 | 0.359 | 0.566 |
| Math Middle | 0.173 | 0.28 | 0.486 | 0.214 | 0.354 | 0.535 | 0.193 | 0.342 | 0.580 |
| Reading/Language <br> Arts Middle | 0.160 | 0.288 | 0.481 | 0.128 | 0.23 | 0.510 | 0.160 | 0.292 | 0.494 |


| Mean | 0.178 | 0.308 | 0.524 | 0.175 | 0.298 | 0.530 | 0.186 | 0.329 | 0.552 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## PP vs. Grate

| Math Elementary | 0.132 | 0.231 | 0.388 | 0.137 | 0.256 | 0.460 | 0.124 | 0.223 | 0.396 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.089 | 0.174 | 0.333 | 0.096 | 0.199 | 0.351 | 0.127 | 0.232 | 0.399 |
| Math Middle | 0.107 | 0.226 | 0.449 | 0.181 | 0.305 | 0.473 | 0.243 | 0.395 | 0.593 |
| Reading/Language <br> Arts Middle | 0.070 | 0.119 | 0.263 | 0.103 | 0.165 | 0.280 | 0.070 | 0.144 | 0.325 |


| Mean | 0.100 | 0.188 | 0.358 | 0.129 | 0.231 | 0.391 | 0.141 | 0.248 | 0.428 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

PP vs. AvGrate

| Math Elementary | 0.167 | 0.269 | 0.485 | 0.153 | 0.285 | 0.518 | 0.153 | 0.289 | 0.503 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.086 | 0.180 | 0.373 | 0.114 | 0.202 | 0.348 | 0.099 | 0.182 | 0.349 |
| Arts Elementary |  |  |  |  |  |  |  |  |  |
| Math Middle | 0.152 | 0.288 | 0.453 | 0.189 | 0.321 | 0.481 | 0.198 | 0.313 | 0.527 |
| Reading/Language <br> Arts Middle | 0.082 | 0.193 | 0.296 | 0.103 | 0.169 | 0.296 | 0.099 | 0.222 | 0.383 |


| Mean | 0.122 | 0.232 | 0.402 | 0.140 | 0.244 | 0.411 | 0.137 | 0.252 | 0.440 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## MLM0 vs. Gain

| Math Elementary | 0.119 | 0.243 | 0.436 | 0.162 | 0.287 | 0.482 | 0.153 | 0.257 | 0.472 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.083 | 0.161 | 0.321 | 0.099 | 0.169 | 0.343 | 0.113 | 0.227 | 0.381 |
| Math Middle | 0.152 | 0.284 | 0.457 | 0.144 | 0.309 | 0.502 | 0.218 | 0.366 | 0.621 |
| Reading/Language <br> Arts Middle | 0.095 | 0.169 | 0.329 | 0.078 | 0.169 | 0.288 | 0.099 | 0.173 | 0.350 |
| Mean | 0.112 | 0.214 | 0.386 | 0.121 | 0.233 | 0.404 | 0.146 | 0.256 | 0.456 |

## MLM0 vs. TM

| Math Elementary | 0.145 | 0.269 | 0.480 | 0.137 | 0.269 | 0.474 | 0.150 | 0.281 | 0.487 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.134 | 0.238 | 0.406 | 0.121 | 0.222 | 0.394 | 0.141 | 0.250 | 0.462 |
| Math Middle | 0.152 | 0.317 | 0.523 | 0.123 | 0.267 | 0.506 | 0.226 | 0.374 | 0.613 |
| Reading/Language <br> Arts Middle | 0.107 | 0.235 | 0.416 | 0.152 | 0.251 | 0.420 | 0.193 | 0.317 | 0.506 |
| Mean | 0.134 | 0.265 | 0.456 | 0.133 | 0.252 | 0.448 | 0.178 | 0.306 | 0.517 |


| MLM0 vs. SGP |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Math Elementary | 0.188 | 0.342 | 0.569 | 0.191 | 0.343 | 0.571 | 0.186 | 0.350 | 0.587 |
| Reading/Language <br> Arts Elementary | 0.184 | 0.311 | 0.538 | 0.164 | 0.278 | 0.464 | 0.169 | 0.291 | 0.525 |
| Math Middle | 0.165 | 0.300 | 0.527 | 0.173 | 0.337 | 0.560 | 0.23 | 0.379 | 0.576 |
| Reading/Language <br> Arts Middle | 0.156 | 0.272 | 0.519 | 0.148 | 0.259 | 0.449 | 0.193 | 0.280 | 0.556 |
| Mean | 0.173 | 0.306 | 0.538 | 0.169 | 0.304 | 0.511 | 0.194 | 0.325 | 0.561 |

MLM0 vs. VAM

| Math Elementary | 0.219 | 0.353 | 0.584 | 0.188 | 0.340 | 0.589 | 0.213 | 0.365 | 0.612 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.177 | 0.325 | 0.579 | 0.171 | 0.295 | 0.520 | 0.177 | 0.328 | 0.548 |
| Arts Elementary |  |  |  |  |  |  |  |  |  |
| Math Middle | 0.165 | 0.313 | 0.543 | 0.189 | 0.325 | 0.560 | 0.235 | 0.374 | 0.593 |
| Reading/Language <br> Arts Middle | 0.152 | 0.251 | 0.498 | 0.111 | 0.267 | 0.514 | 0.160 | 0.317 | 0.531 |


| Mean | 0.178 | 0.310 | 0.551 | 0.165 | 0.307 | 0.546 | 0.196 | 0.346 | 0.571 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

MLM0 vs. Grate

| Math Elementary | 0.116 | 0.210 | 0.381 | 0.135 | 0.284 | 0.472 | 0.120 | 0.229 | 0.408 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.075 | 0.149 | 0.298 | 0.089 | 0.180 | 0.315 | 0.099 | 0.214 | 0.397 |
| Math Middle | 0.160 | 0.284 | 0.457 | 0.156 | 0.292 | 0.506 | 0.292 | 0.449 | 0.691 |
| Reading/Language <br> Arts Middle | 0.058 | 0.119 | 0.272 | 0.078 | 0.165 | 0.280 | 0.111 | 0.173 | 0.313 |
| Mean | 0.102 | 0.190 | 0.352 | 0.114 | 0.230 | 0.393 | 0.156 | 0.266 | 0.452 |

MLM0 vs.
AvGrate
Math Elementary
$\begin{array}{lll}0.198 & 0.312 & 0.510\end{array}$
$\begin{array}{lll}0.167 & 0.309 & 0.528\end{array}$
$\begin{array}{lll}0.178 & 0.297 & 0.530\end{array}$
$\begin{array}{llllllllll}\text { Reading/Language } & 0.086 & 0.167 & 0.341 & 0.096 & 0.187 & 0.358 & 0.114 & 0.194 & 0.349\end{array}$ Arts Elementary

| Math Middle | 0.193 | 0.333 | 0.502 | 0.156 | 0.280 | 0.457 | 0.193 | 0.313 | 0.490 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Middle | 0.095 | 0.165 | 0.300 | 0.099 | 0.173 | 0.296 | 0.119 | 0.210 | 0.399 |
| Mean | 0.143 | 0.244 | 0.413 | 0.130 | 0.237 | 0.410 | 0.151 | 0.254 | 0.442 |

## Gain vs. TM

| Math Elementary | 0.403 | 0.614 | 0.866 | 0.404 | 0.642 | 0.884 | 0.406 | 0.639 | 0.875 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.272 | 0.439 | 0.697 | 0.281 | 0.464 | 0.738 | 0.091 | 0.180 | 0.329 |
| Math Middle | 0.395 | 0.597 | 0.831 | 0.387 | 0.613 | 0.848 | 0.481 | 0.700 | 0.918 |
| Reading/Language <br> Arts Middle | 0.226 | 0.374 | 0.588 | 0.202 | 0.412 | 0.650 | 0.267 | 0.461 | 0.634 |
| Mean | 0.324 | 0.506 | 0.745 | 0.318 | 0.533 | 0.780 | 0.311 | 0.495 | 0.689 |

## Gain vs. SGP

| Math Elementary | 0.315 | 0.490 | 0.777 | 0.429 | 0.639 | 0.865 | 0.327 | 0.526 | 0.795 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.250 | 0.401 | 0.594 | 0.228 | 0.389 | 0.647 | 0.141 | 0.233 | 0.416 |
| Math Middle | 0.329 | 0.560 | 0.798 | 0.383 | 0.613 | 0.844 | 0.469 | 0.675 | 0.897 |
| Reading/Language <br> Arts Middle | 0.226 | 0.370 | 0.642 | 0.247 | 0.391 | 0.601 | 0.280 | 0.387 | 0.646 |


| Mean | 0.280 | 0.455 | 0.703 | 0.322 | 0.508 | 0.739 | 0.304 | 0.455 | 0.688 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Gain vs. VAM

| Math Elementary | 0.292 | 0.523 | 0.795 | 0.436 | 0.670 | 0.893 | 0.340 | 0.561 | 0.818 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.220 | 0.376 | 0.616 | 0.243 | 0.399 | 0.666 | 0.113 | 0.228 | 0.417 |
| Math Middle | 0.395 | 0.630 | 0.848 | 0.416 | 0.609 | 0.868 | 0.506 | 0.708 | 0.934 |

$\begin{array}{llllllllll}\text { Reading/Language } & 0.206 & 0.346 & 0.650 & 0.206 & 0.366 & 0.638 & 0.255 & 0.391 & 0.658\end{array}$ Arts Middle

| Mean | 0.278 | 0.469 | 0.727 | 0.325 | 0.511 | 0.766 | 0.304 | 0.472 | 0.707 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Gain vs. Grate

| Math Elementary | 0.512 | 0.795 | 0.979 | 0.660 | 0.866 | 0.987 | 0.578 | 0.807 | 0.974 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.424 | 0.689 | 0.912 | 0.500 | 0.743 | 0.960 | 0.079 | 0.139 | 0.272 |
| Arts Elementary |  |  |  |  |  |  |  |  |  |
| Math Middle | 0.498 | 0.765 | 0.942 | 0.551 | 0.798 | 0.979 | 0.609 | 0.885 | 0.992 |
| Reading/Language <br> Arts Middle | 0.424 | 0.704 | 0.938 | 0.436 | 0.704 | 0.901 | 0.543 | 0.811 | 0.975 |


| Mean | 0.464 | 0.738 | 0.943 | 0.537 | 0.778 | 0.957 | 0.452 | 0.661 | 0.803 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Gain vs. AvGrate

| Math Elementary | 0.200 | 0.351 | 0.558 | 0.241 | 0.432 | 0.677 | 0.193 | 0.328 | 0.556 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.204 | 0.353 | 0.545 | 0.175 | 0.318 | 0.551 | 0.215 | 0.404 | 0.616 |
| Math Middle | 0.226 | 0.366 | 0.556 | 0.272 | 0.362 | 0.617 | 0.296 | 0.469 | 0.704 |
| Reading/Language <br> Arts Middle | 0.222 | 0.317 | 0.605 | 0.214 | 0.374 | 0.588 | 0.276 | 0.428 | 0.658 |


| Mean | 0.213 | 0.347 | 0.566 | 0.226 | 0.372 | 0.608 | 0.245 | 0.407 | 0.634 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## TM vs. SGP

| Math Elementary | 0.315 | 0.485 | 0.774 | 0.363 | 0.533 | 0.789 | 0.309 | 0.517 | 0.784 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.240 | 0.424 | 0.639 | 0.247 | 0.394 | 0.619 | 0.281 | 0.452 | 0.697 |
| Arts Elementary |  |  |  |  |  |  |  |  |  |
| Math Middle | 0.235 | 0.444 | 0.712 | 0.379 | 0.584 | 0.782 | 0.391 | 0.572 | 0.835 |
| Reading/Language | 0.337 | 0.502 | 0.745 | 0.272 | 0.399 | 0.667 | 0.333 | 0.490 | 0.737 |
| Arts Middle |  |  |  |  |  |  |  |  |  |


| Mean | 0.282 | 0.464 | 0.718 | 0.315 | 0.478 | 0.714 | 0.328 | 0.508 | 0.763 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

TM vs. VAM

| Math Elementary | 0.300 | 0.492 | 0.769 | 0.351 | 0.554 | 0.799 | 0.330 | 0.513 | 0.781 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.232 | 0.387 | 0.647 | 0.233 | 0.386 | 0.651 | 0.273 | 0.430 | 0.689 |
| Arts Elementary |  |  |  |  |  |  |  |  |  |
| Math Middle | 0.263 | 0.465 | 0.737 | 0.350 | 0.576 | 0.798 | 0.387 | 0.572 | 0.840 |
| Reading/Language <br> Arts Middle | 0.259 | 0.449 | 0.733 | 0.235 | 0.383 | 0.675 | 0.317 | 0.498 | 0.774 |


| Mean | 0.264 | 0.448 | 0.722 | 0.292 | 0.475 | 0.731 | 0.327 | 0.503 | 0.771 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

TM vs. Grate

| Math Elementary | 0.317 | 0.526 | 0.792 | 0.360 | 0.554 | 0.838 | 0.335 | 0.551 | 0.790 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.215 | 0.373 | 0.613 | 0.212 | 0.396 | 0.671 | 0.257 | 0.422 | 0.684 |
| Math Middle | 0.309 | 0.547 | 0.790 | 0.337 | 0.523 | 0.802 | 0.457 | 0.683 | 0.872 |
| Reading/Language <br> Arts Middle | 0.173 | 0.313 | 0.514 | 0.177 | 0.362 | 0.543 | 0.259 | 0.366 | 0.601 |


| Mean | 0.254 | 0.440 | 0.677 | 0.272 | 0.459 | 0.714 | 0.327 | 0.506 | 0.737 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

TM vs. AvGrate

| Math Elementary | 0.185 | 0.345 | 0.543 | 0.233 | 0.394 | 0.640 | 0.186 | 0.328 | 0.543 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language | 0.142 | 0.288 | 0.459 | 0.179 | 0.298 | 0.526 | 0.177 | 0.290 | 0.475 |
| Arts Elementary |  |  |  |  |  |  |  |  |  |
| Math Middle | 0.218 | 0.333 | 0.498 | 0.218 | 0.403 | 0.626 | 0.239 | 0.412 | 0.667 |
| Reading/Language <br> Arts Middle | 0.160 | 0.272 | 0.514 | 0.123 | 0.276 | 0.444 | 0.206 | 0.346 | 0.535 |


| Mean | 0.176 | 0.310 | 0.504 | 0.188 | 0.343 | 0.559 | 0.202 | 0.344 | 0.555 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## SGP vs. VAM

| Math Elementary | 0.583 | 0.830 | 0.972 | 0.579 | 0.828 | 0.969 | 0.564 | 0.807 | 0.980 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.417 | 0.671 | 0.921 | 0.444 | 0.685 | 0.897 | 0.429 | 0.682 | 0.904 |
| Math Middle | 0.564 | 0.794 | 0.959 | 0.609 | 0.856 | 0.984 | 0.621 | 0.848 | 0.979 |
| Reading/Language <br> Arts Middle | 0.424 | 0.671 | 0.926 | 0.420 | 0.700 | 0.905 | 0.432 | 0.728 | 0.930 |
| Mean | 0.497 | 0.742 | 0.944 | 0.513 | 0.767 | 0.939 | 0.511 | 0.766 | 0.948 |

SGP vs. Grate

| Math Elementary | 0.221 | 0.381 | 0.634 | 0.322 | 0.528 | 0.748 | 0.224 | 0.408 | 0.653 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.164 | 0.293 | 0.512 | 0.152 | 0.315 | 0.540 | 0.247 | 0.379 | 0.604 |
| Math Middle | 0.243 | 0.379 | 0.691 | 0.317 | 0.457 | 0.695 | 0.387 | 0.556 | 0.782 |
| Reading/Language <br> Arts Middle | 0.177 | 0.292 | 0.502 | 0.144 | 0.276 | 0.490 | 0.210 | 0.325 | 0.527 |
| Mean | 0.201 | 0.336 | 0.585 | 0.234 | 0.394 | 0.618 | 0.267 | 0.417 | 0.642 |

SGP vs. AvGrate

| Math Elementary | 0.282 | 0.487 | 0.731 | 0.337 | 0.589 | 0.818 | 0.333 | 0.502 | 0.761 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.185 | 0.316 | 0.543 | 0.224 | 0.374 | 0.593 | 0.238 | 0.389 | 0.611 |
| Math Middle | 0.296 | 0.477 | 0.745 | 0.329 | 0.560 | 0.802 | 0.387 | 0.630 | 0.872 |
| Reading/Language <br> Arts Middle | 0.210 | 0.362 | 0.597 | 0.202 | 0.354 | 0.613 | 0.255 | 0.391 | 0.634 |
| Mean | 0.243 | 0.410 | 0.654 | 0.273 | 0.469 | 0.706 | 0.303 | 0.478 | 0.720 |

VAM vs. Grate
$\begin{array}{llllllllll}\text { Math Elementary } & 0.215 & 0.373 & 0.624 & 0.332 & 0.531 & 0.771 & 0.254 & 0.416 & 0.672\end{array}$

| Reading/Language | 0.172 | 0.316 | 0.512 | 0.209 | 0.353 | 0.581 | 0.248 | 0.396 | 0.627 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Arts Elementary |  |  |  |  |  |  |  |  |  |

Grate vs. AvGrate

| Math Elementary | 0.150 | 0.267 | 0.459 | 0.219 | 0.338 | 0.586 | 0.137 | 0.257 | 0.459 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Reading/Language <br> Arts Elementary | 0.136 | 0.253 | 0.430 | 0.139 | 0.260 | 0.434 | 0.139 | 0.255 | 0.449 |
| Math Middle | 0.169 | 0.296 | 0.461 | 0.214 | 0.300 | 0.490 | 0.230 | 0.391 | 0.601 |
| Reading/Language <br> Arts Middle | 0.202 | 0.333 | 0.568 | 0.181 | 0.288 | 0.486 | 0.189 | 0.391 | 0.601 |
| Mean | 0.164 | 0.287 | 0.480 | 0.188 | 0.296 | 0.499 | 0.174 | 0.324 | 0.528 |

## Appendix E

## RMSD in School Ranks for Pairs of School Performance Models for each Individual Cohort by Content Area and Grade Level Band.

Elementary School Mathematics: Cohort 1

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 15.770 | 37.362 | 34.105 | 29.798 | 29.045 | 39.441 | 34.357 |
| MLM0 |  | 37.581 | 34.712 | 28.086 | 27.087 | 40.005 | 32.912 |
| Gain |  |  | 13.586 | 17.328 | 16.493 | 8.491 | 28.533 |
| TM |  |  |  | 18.316 | 17.633 | 16.537 | 29.001 |
| SGP |  |  |  |  | 8.358 | 23.251 | 20.655 |
| VAM |  |  |  |  |  | 22.979 | 19.137 |
| Grate |  |  |  |  |  |  | 34.628 |

Elementary School Mathematics: Cohort 2

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 14.395 | 32.726 | 33.384 | 28.644 | 27.823 | 34.156 | 31.510 |
| MLM0 |  | 31.685 | 33.452 | 27.287 | 26.152 | 33.020 | 30.914 |
| Gain |  |  | 12.974 | 13.846 | 12.127 | 6.928 | 23.014 |
| TM |  |  |  | 17.736 | 17.345 | 14.738 | 24.819 |
| SGP |  |  |  |  | 8.376 | 18.687 | 16.332 |
| VAM |  |  |  |  |  | 17.860 | 14.033 |
| Grate |  |  |  |  |  |  | 28.523 |

Elementary School Mathematics: Cohort 3

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | ---: | :--- |
| PP | 14.438 | 34.826 | 31.582 | 29.163 | 27.95 | 37.177 | 30.428 |
| MLM0 |  | 33.463 | 31.036 | 26.362 | 25.182 | 36.223 | 28.276 |
| Gain |  |  | 13.221 | 16.738 | 15.247 | 8.409 | 29.121 |
| TM |  |  |  | 17.213 | 16.842 | 16.581 | 28.739 |
| SGP |  |  |  |  | 8.232 | 23.134 | 18.582 |


| VAM |  |  |  |  |  | 22.268 | $\begin{aligned} & 17.376 \\ & 35.168 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Grate |  |  |  |  |  |  |  |
| Elementary School Reading/Language Arts: Cohort 1 |  |  |  |  |  |  |  |
| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| PP | 15.540 | 41.213 | 34.408 | 29.400 | 27.321 | 43.555 | 42.161 |
| MLM0 |  | 43.497 | 35.963 | 29.225 | 27.463 | 45.584 | 43.963 |
| Gain |  |  | 22.777 | 25.344 | 24.121 | 11.436 | 29.191 |
| TM |  |  |  | 22.777 | 22.356 | 25.866 | 33.432 |
| SGP |  |  |  |  | 11.359 | 31.683 | 28.953 |
| VAM |  |  |  |  |  | 30.928 | 28.344 |
| Grate |  |  |  |  |  |  | 36.431 |

Elementary School Reading/Language Arts: Cohort 2

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 15.237 | 39.573 | 36.531 | 31.045 | 29.042 | 40.759 | 40.435 |
| MLM0 |  | 41.291 | 38.112 | 30.641 | 28.763 | 42.498 | 40.938 |
| Gain |  |  | 20.322 | 21.984 | 20.109 | 9.431 | 28.105 |
| TM |  |  |  | 23.757 | 23.045 | 22.685 | 30.209 |
| SGP |  |  |  |  | 12.271 | 26.996 | 24.897 |
| VAM |  |  |  |  |  | 25.955 | 23.274 |
| Grate |  |  |  |  |  |  | 34.614 |

Elementary School Reading/Language Arts: Cohort 3

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 13.361 | 42.724 | 33.727 | 30.142 | 28.365 | 38.305 | 41.723 |
| MLM0 |  | 42.277 | 34.736 | 30.326 | 28.634 | 39.893 | 42.711 |
| Gain |  |  | 44.548 | 39.077 | 38.925 | 49.566 | 25.217 |
| TM |  |  |  | 21.761 | 21.312 | 21.682 | 31.506 |
| SGP |  |  |  |  | 11.974 | 25.923 | 25.274 |
| VAM |  |  |  |  |  | 24.214 | 23.890 |
| Grate |  |  |  |  |  |  | 33.782 |


| Middle School Mathematics: Cohort 1 |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| PP | 15.945 | 33.532 | 29.275 | 31.237 | 31.078 | 33.991 | 34.467 |
| MLM0 |  | 31.716 | 30.267 | 28.905 | 28.418 | 32.702 | 32.596 |
| Gain |  |  | 15.570 | 17.226 | 15.180 | 9.810 | 29.276 |
| TM |  |  |  | 21.650 | 20.802 | 16.673 | 31.588 |
| SGP |  |  |  |  | 9.639 | 24.035 | 18.819 |
| VAM |  |  |  |  |  | 22.930 | 16.925 |
| Grate |  |  |  |  |  |  | 35.983 |

Middle School Mathematics: Cohort 2

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 15.635 | 30.273 | 27.086 | 27.474 | 27.691 | 30.347 | 33.333 |
| MLM0 |  | 30.719 | 29.502 | 27.656 | 27.321 | 30.368 | 33.654 |
| Gain |  |  | 15.684 | 13.993 | 12.869 | 8.252 | 24.499 |
| TM |  |  |  | 17.324 | 17.193 | 17.646 | 25.730 |
| SGP |  |  |  |  | 7.731 | 19.772 | 16.862 |
| VAM |  |  |  |  |  | 18.960 | 14.753 |
| Grate |  |  |  |  |  |  | 30.439 |

Middle School Mathematics: Cohort 3

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 17.076 | 26.629 | 24.410 | 27.029 | 26.004 | 25.949 | 28.927 |
| MLM0 |  | 23.594 | 23.467 | 24.903 | 24.606 | 21.557 | 29.608 |
| Gain |  |  | 12.116 | 12.830 | 10.747 | 6.916 | 20.965 |
| TM |  |  |  | 15.701 | 14.937 | 13.012 | 22.505 |
| SGP |  |  |  |  | 7.620 | 16.842 | 13.090 |
| VAM |  |  |  |  |  | 15.846 | 11.246 |
| Grate |  |  |  |  |  |  | 25.664 |

Middle School Reading/Language Arts: Cohort 1

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PP | 13.241 | 43.882 | 32.089 | 32.422 | 33.161 | 46.984 | 44.585 |
| MLM0 |  | 46.167 | 35.268 | 33.305 | 34.104 | 49.012 | 45.698 |
| Gain |  |  | 24.977 | 24.299 | 22.190 | 11.217 | 25.328 |
| TM |  |  |  | 20.479 | 20.045 | 29.293 | 31.687 |
| SGP |  |  |  |  | 11.441 | 30.771 | 26.530 |
| VAM |  |  |  |  |  | 29.010 | 23.190 |
| Grate |  |  |  |  |  |  | 30.048 |

Middle School Reading/Language Arts: Cohort 2

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| PP | 15.000 | 44.032 | 34.833 | 32.958 | 32.319 | 46.304 | 45.287 |
| MLM0 |  | 46.575 | 37.457 | 34.303 | 33.357 | 48.333 | 47.229 |
| Gain |  |  | 23.159 | 25.486 | 24.178 | 11.342 | 26.658 |
| TM |  |  |  | 24.126 | 22.259 | 26.615 | 33.678 |
| SGP |  |  |  |  | 11.744 | 32.150 | 26.751 |
| VAM |  |  |  |  |  | 30.725 | 26.232 |
| Grate |  |  |  |  |  |  | 32.473 |

Middle School Reading/Language Arts: Cohort 3

| Model | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| PP | 12.169 | 42.661 | 32.093 | 30.448 | 29.671 | 45.404 | 40.724 |
| MLM0 |  | 43.755 | 32.510 | 29.891 | 29.391 | 46.377 | 41.262 |
| Gain |  |  | 23.650 | 23.746 | 22.771 | 8.753 | 24.015 |
| TM |  |  |  | 19.919 | 18.565 | 26.819 | 28.573 |
| SGP |  |  |  |  | 10.938 | 28.795 | 23.796 |
| VAM |  |  |  |  |  | 28.036 | 20.678 |
| Grate |  |  |  |  |  |  | 27.729 |

## Appendix F

## Correlations of School Ranks with School Composition Variables by Content Area and Grade Level Band for each Individual Cohort.

Elementary School Mathematics: Cohort 1

| Model | EDS | EL | SWD | Female | Ethnic Minority | School Size | Mean |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PP | -0.490 | -0.351 | -0.212 | -0.025 | -0.273 | 0.124 | -0.204 |
| MLM0 | -0.599 | -0.325 | -0.185 | -0.045 | -0.282 | 0.224 | -0.202 |
| Gain | 0.105 | 0.164 | 0.066 | -0.022 | 0.098 | 0.181 | 0.099 |
| TM | -0.001 | 0.107 | 0.004 | -0.033 | 0.042 | 0.185 | 0.051 |
| SGP | -0.135 | 0.030 | -0.025 | -0.044 | 0.017 | 0.248 | 0.015 |
| VAM | -0.153 | 0.029 | -0.029 | -0.023 | 0.008 | 0.265 | 0.016 |
| Grate | 0.126 | 0.154 | 0.089 | -0.018 | 0.076 | 0.132 | 0.093 |
| AvGrate | 0.013 | 0.139 | -0.008 | 0.001 | 0.134 | 0.223 | 0.084 |

Elementary School Mathematics: Cohort 2

|  |  |  |  | Ethnic |  |  | School |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.548 | -0.338 | -0.213 | 0.045 | -0.270 | 0.142 | -0.197 |
| MLM0 | -0.626 | -0.315 | -0.198 | 0.033 | -0.271 | 0.219 | -0.193 |
| Gain | -0.042 | 0.054 | 0.015 | 0.036 | 0.033 | 0.116 | 0.035 |
| TM | 0.002 | 0.056 | 0.003 | 0.047 | 0.029 | 0.088 | 0.038 |
| SGP | -0.122 | 0.011 | -0.014 | 0.035 | 0.016 | 0.144 | 0.012 |
| VAM | -0.147 | 0.010 | -0.034 | 0.059 | 0.015 | 0.168 | 0.012 |
| Grate | -0.057 | 0.022 | 0.017 | 0.024 | -0.003 | 0.076 | 0.013 |
| AvGrate | 0.003 | 0.104 | -0.007 | 0.073 | 0.103 | 0.158 | 0.072 |

Elementary School Mathematics: Cohort 3

| Model | EDS | EL | SWD | Female | Ethnic | Minority | School |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Size | Mean |  |  |  |  |  |  |
| PP | -0.539 | -0.280 | -0.191 | -0.018 | -0.303 | 0.103 | -0.205 |
| MLM0 | -0.622 | -0.262 | -0.169 | -0.016 | -0.262 | 0.195 | -0.189 |
| Gain | -0.109 | -0.058 | -0.057 | -0.021 | -0.067 | 0.046 | -0.044 |
| TM | -0.160 | -0.104 | -0.039 | -0.046 | -0.108 | 0.034 | -0.070 |
| SGP | -0.220 | -0.079 | -0.077 | -0.007 | -0.074 | 0.123 | -0.056 |
| VAM | -0.248 | -0.090 | -0.097 | 0.004 | -0.097 | 0.129 | -0.066 |
| Grate | -0.087 | -0.073 | -0.031 | -0.038 | -0.079 | 0.005 | -0.050 |
| AvGrate | -0.104 | 0.015 | -0.066 | 0.039 | 0.005 | 0.139 | 0.005 |

Elementary School Reading/Language Arts: Cohort 1

|  |  |  |  |  | Ethnic | School |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.555 | -0.510 | -0.181 | -0.034 | -0.424 | 0.028 | -0.279 |
| MLM0 | -0.681 | -0.475 | -0.178 | -0.029 | -0.418 | 0.136 | -0.274 |
| Gain | 0.222 | 0.183 | 0.120 | -0.029 | 0.154 | 0.091 | 0.124 |
| TM | -0.092 | 0.030 | 0.076 | -0.085 | 0.043 | 0.156 | 0.021 |
| SGP | -0.224 | -0.069 | -0.032 | 0.005 | -0.079 | 0.183 | -0.036 |
| VAM | -0.279 | -0.120 | -0.035 | -0.016 | -0.119 | 0.195 | -0.062 |
| Grate | 0.252 | 0.157 | 0.146 | -0.017 | 0.131 | 0.052 | 0.120 |
| AvGrate | 0.234 | 0.311 | 0.055 | -0.002 | 0.233 | 0.053 | 0.147 |

Elementary School Reading/Language Arts: Cohort 2

|  |  |  |  | Ethnic |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.626 | -0.488 | -0.248 | 0.012 | -0.414 | 0.052 | -0.285 |
| MLM0 | -0.741 | -0.495 | -0.225 | 0.015 | -0.440 | 0.134 | -0.292 |


| Gain | 0.097 | 0.180 | 0.041 | -0.013 | 0.124 | 0.036 | 0.078 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TM | -0.056 | 0.082 | 0.032 | -0.004 | 0.059 | 0.085 | 0.033 |
| SGP | -0.233 | -0.051 | -0.079 | -0.001 | -0.066 | 0.108 | -0.054 |
| VAM | -0.268 | -0.066 | -0.083 | 0.012 | -0.089 | 0.123 | -0.062 |
| Grate | 0.098 | 0.138 | 0.048 | -0.013 | 0.094 | -0.003 | 0.060 |
| AvGrate | 0.187 | 0.266 | 0.045 | 0.013 | 0.184 | 0.093 | 0.131 |

Elementary School Reading/Language Arts: Cohort 3

|  |  |  |  | Ethnic |  |  | School |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.648 | -0.476 | -0.173 | 0.029 | -0.440 | 0.041 | -0.278 |
| MLM0 | -0.745 | -0.470 | -0.141 | 0.002 | -0.452 | 0.097 | -0.285 |
| Gain | 0.141 | 0.159 | 0.088 | -0.040 | 0.123 | 0.054 | 0.088 |
| TM | -0.107 | -0.019 | 0.008 | 0.010 | -0.049 | 0.026 | -0.022 |
| SGP | -0.218 | -0.066 | -0.019 | -0.002 | -0.102 | 0.047 | -0.060 |
| VAM | -0.246 | -0.099 | -0.028 | 0.022 | -0.121 | 0.061 | -0.068 |
| Grate | 0.066 | 0.053 | -0.021 | 0.031 | 0.042 | -0.028 | 0.024 |
| AvGrate | 0.252 | 0.243 | 0.080 | 0.003 | 0.188 | 0.017 | 0.130 |

Middle School Mathematics: Cohort 1

|  |  |  |  | Ethnic |  |  | School |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.438 | -0.154 | -0.242 | -0.055 | -0.262 | 0.135 | -0.169 |
| MLM0 | -0.495 | -0.065 | -0.162 | -0.101 | -0.167 | 0.208 | -0.130 |
| Gain | -0.058 | 0.128 | 0.048 | -0.078 | 0.163 | 0.176 | 0.063 |
| TM | -0.091 | 0.092 | -0.031 | -0.076 | 0.084 | 0.186 | 0.027 |
| SGP | -0.015 | 0.185 | 0.067 | -0.044 | 0.163 | 0.180 | 0.089 |
| VAM | -0.026 | 0.170 | 0.053 | -0.054 | 0.143 | 0.191 | 0.080 |
| Grate | -0.123 | 0.063 | 0.010 | -0.094 | 0.113 | 0.148 | 0.020 |

$\begin{array}{llllllll}\text { AvGrate } & 0.093 & 0.180 & 0.066 & -0.006 & 0.130 & 0.109 & 0.095\end{array}$

Middle School Mathematics: Cohort 2

|  |  |  |  | Ethnic |  |  | School |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.377 | -0.266 | -0.301 | 0.106 | -0.255 | 0.081 | -0.169 |
| MLM0 | -0.481 | -0.197 | -0.177 | 0.121 | -0.174 | 0.167 | -0.124 |
| Gain | 0.056 | 0.028 | 0.000 | 0.007 | -0.031 | 0.045 | 0.018 |
| TM | -0.038 | -0.025 | -0.081 | 0.022 | -0.085 | 0.100 | -0.018 |
| SGP | 0.021 | 0.043 | -0.048 | 0.025 | -0.008 | 0.105 | 0.023 |
| VAM | 0.027 | 0.044 | -0.033 | 0.039 | 0.001 | 0.105 | 0.030 |
| Grate | -0.026 | -0.026 | -0.016 | 0.006 | -0.066 | 0.029 | -0.016 |
| AvGrate | 0.171 | 0.158 | 0.006 | 0.039 | 0.080 | 0.123 | 0.096 |

Middle School Mathematics: Cohort 3

|  |  |  |  | Ethnic |  |  | School |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.340 | -0.214 | -0.254 | 0.071 | -0.121 | 0.140 | -0.120 |
| MLM0 | -0.487 | -0.187 | -0.194 | -0.007 | -0.083 | 0.235 | -0.120 |
| Gain | -0.100 | -0.023 | -0.085 | 0.030 | 0.044 | 0.218 | 0.014 |
| TM | -0.152 | -0.041 | -0.097 | 0.023 | 0.014 | 0.190 | -0.010 |
| SGP | -0.050 | 0.026 | -0.066 | 0.017 | 0.089 | 0.235 | 0.042 |
| VAM | -0.033 | 0.008 | -0.088 | 0.021 | 0.078 | 0.208 | 0.032 |
| Grate | -0.189 | -0.061 | -0.106 | 0.026 | 0.002 | 0.225 | -0.017 |
| AvGrate | 0.093 | 0.065 | -0.067 | 0.025 | 0.125 | 0.157 | 0.066 |

Middle School Reading/Language Arts: Cohort 1

| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PP | -0.558 | -0.350 | -0.318 | 0.165 | -0.398 | 0.090 | -0.228 |
| MLM0 | -0.673 | -0.318 | -0.289 | 0.085 | -0.386 | 0.128 | -0.242 |
| Gain | 0.327 | 0.166 | 0.113 | 0.002 | 0.184 | -0.005 | 0.131 |
| TM | -0.023 | 0.013 | -0.045 | 0.076 | -0.045 | 0.106 | 0.014 |
| SGP | -0.059 | 0.033 | -0.031 | 0.046 | -0.017 | 0.103 | 0.012 |
| VAM | -0.021 | 0.052 | -0.034 | 0.010 | -0.018 | 0.096 | 0.014 |
| Grate | 0.390 | 0.192 | 0.163 | -0.039 | 0.227 | -0.010 | 0.154 |
| AvGrate | 0.412 | 0.314 | 0.112 | -0.038 | 0.242 | 0.044 | 0.181 |

Middle School Reading/Language Arts: Cohort 2

| Model | EDS | EL | SWD | Female | Ethnic <br> Minority | School Size | Mean |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PP | -0.526 | -0.446 | -0.221 | 0.204 | -0.447 | -0.003 | -0.240 |
| MLM0 | -0.682 | -0.434 | -0.185 | 0.188 | -0.440 | 0.084 | -0.245 |
| Gain | 0.395 | 0.259 | 0.133 | -0.050 | 0.161 | -0.021 | 0.146 |
| TM | 0.052 | 0.058 | 0.062 | 0.048 | -0.013 | 0.053 | 0.043 |
| SGP | -0.013 | 0.017 | 0.015 | 0.043 | -0.031 | 0.085 | 0.019 |
| VAM | -0.028 | 0.014 | -0.012 | 0.071 | -0.079 | 0.049 | 0.002 |
| Grate | 0.395 | 0.245 | 0.139 | -0.081 | 0.139 | -0.052 | 0.131 |
| AvGrate | 0.469 | 0.332 | 0.148 | -0.051 | 0.268 | 0.011 | 0.196 |

Middle School Reading/Language Arts: Cohort 3

|  |  |  |  | Ethnic |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| School |  |  |  |  |  |  |  |
| Model | EDS | EL | SWD | Female | Minority | Size | Mean |
| PP | -0.594 | -0.360 | -0.275 | 0.032 | -0.358 | 0.071 | -0.247 |
| MLM0 | -0.705 | -0.354 | -0.249 | 0.051 | -0.357 | 0.104 | -0.252 |


| Gain | 0.292 | 0.257 | 0.163 | -0.014 | 0.230 | 0.117 | 0.174 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TM | -0.123 | 0.016 | 0.034 | 0.006 | 0.053 | 0.251 | 0.040 |
| SGP | -0.153 | 0.030 | -0.047 | 0.064 | -0.009 | 0.168 | 0.009 |
| VAM | -0.117 | 0.037 | -0.009 | 0.037 | 0.007 | 0.165 | 0.020 |
| Grate | 0.358 | 0.276 | 0.194 | -0.044 | 0.255 | 0.089 | 0.188 |
| AvGrate | 0.313 | 0.288 | 0.135 | 0.023 | 0.171 | 0.059 | 0.165 |

## Appendix G

## Correlations of School Performance Model Estimates with School Percentage SWD for each Individual Cohort by Content Area and Grade Level Band.

Elementary School Mathematics

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| 1 | -0.212 | -0.185 | 0.066 | 0.004 | -0.025 | -0.029 | 0.089 | -0.008 |
| 2 | -0.213 | -0.198 | 0.015 | 0.003 | -0.014 | -0.034 | 0.017 | -0.007 |
| 3 | -0.191 | -0.169 | -0.057 | -0.039 | -0.077 | -0.097 | -0.031 | -0.066 |

Elementary School Reading/Language Arts

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -0.181 | -0.178 | 0.120 | 0.076 | -0.032 | -0.035 | 0.146 | 0.055 |
| 2 | -0.248 | -0.225 | 0.041 | 0.032 | -0.079 | -0.083 | 0.048 | 0.045 |
| 3 | -0.173 | -0.141 | 0.088 | 0.008 | -0.019 | -0.028 | -0.021 | 0.080 |

Middle School Mathematics

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -0.242 | -0.162 | 0.048 | -0.031 | 0.067 | 0.053 | 0.010 | 0.066 |
| 2 | -0.301 | -0.177 | 0.000 | -0.081 | -0.048 | -0.033 | -0.016 | 0.006 |
| 3 | -0.254 | -0.194 | -0.085 | -0.097 | -0.066 | -0.088 | -0.106 | -0.067 |

Middle School Reading/Language Arts

| Cohort | PP | MLM0 | Gain | TM | SGP | VAM | Grate | AvGrate |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -0.318 | -0.289 | 0.113 | -0.045 | -0.031 | -0.034 | 0.163 | 0.112 |
| 2 | -0.221 | -0.185 | 0.133 | 0.062 | 0.015 | -0.012 | 0.139 | 0.148 |
| 3 | -0.275 | -0.249 | 0.163 | 0.034 | -0.047 | -0.009 | 0.194 | 0.135 |


[^0]:    ${ }^{\text {a }}$ University of Oregon
    ${ }^{\mathrm{b}}$ Arizona State University
    ${ }^{\text {c }}$ Indiana University

